






# New low mass ratio contact binaries in the Catalina Sky Survey

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## ABSTRACT

We present the identification and photometric analysis of 30 new low mass ratio (LMR) totally eclipsing contact binaries found in Catalina Sky Survey data. The LMR candidates are identified using Fourier coefficients and visual inspection. We perform a detailed scan in the parameter plane of mass ratio ( $q$ ) versus inclination ( $i$ ) using PHOEBE -0.31 scripter to derive the best ( $q$ ,  $i$ ) pair for the initial models. The relative physical parameters are determined from the final model of each system. A Monte Carlo approach was adopted to derive the parameter errors. The resulting parameters confirm the identification. The approximate absolute physical parameters of the systems are estimated based on the light-curve solutions and *Gaia* Early Data Release 3 distances. 12 out of 30 new systems have fill-out factors  $f > 50$  per cent and  $q \leq 0.25$  (deep contact LMR systems), and eight of them, to within errors, are extreme LMR deep systems with  $q \leq 0.1$ . We discuss the evolutionary status of the 30 LMR systems in comparison with the most updated catalogue of LMR systems from the literature. The scenario of the LMR systems as pre-merger candidates forming fast rotating stars is investigated for all systems, new and old, based both on Hut's stability criteria and critical instability mass ratio ( $q_{\text{inst}}$ ) relation. CSS\_J075848.2+125656, with  $q/q_{\text{inst}} = 1.23 \pm 0.23$ , and CSS\_J093010.1–021624, with  $q/q_{\text{inst}} = 1.25 \pm 0.23$ , can be considered as merger candidates.

**Key words:** surveys – binaries: eclipsing – binaries: close – stars: evolution – stars: fundamental parameters.

## 1 INTRODUCTION

Eclipsing binary systems of EW light-curve type (EWs) with extreme low mass ratios challenge the current theoretical models since the latter predict coalescence into a single star (Robertson & Eggleton 1977; Eggleton 2010a, and references therein). In at least one case, V1309 Sco, such a merger event has been directly observed (Nakano et al. 2008). This defined a distinct new class of luminous red novae that was later attributed, upon analysis of archival photometric data from the Optical Gravitational Lensing Experiment (OGLE; Udalski 2003), to the merging components of a cool overcontact eclipsing binary system with a decreasing orbital period (Tylenda et al. 2011). What triggers the binary to merge is still controversial. The widely accepted scenario is Darwin's instability model (Darwin 1879), which implies that the merger happens when the spin angular momentum of the system is more than one-third of the orbital angular momentum (Hut 1980; Rasio 1995). When the binary mass ratio is extremely small and the secondary component has extremely small

mass, it can no longer continue to corotate synchronously with the primary via the tidal interaction. As a consequence of the secondary's higher angular velocity, angular momentum is transported rapidly from the orbital motion to the primary's spin, causing the orbit to shrink and the period to shorten, until the engulfment of the secondary. Models suggest that single stars (FK Com and blue straggler type) could be the result of this coalescence (Rasio 1995; Stępień 2006; Stępień & Kiraga 2015). In addition, both the loss of mass and angular momentum through magnetic winds (Stępień 2006, 2009; Stępień & Gazeas 2012) and the presence of other companion(s) play a crucial role in the merging process. Since most stars are in binaries, and a significant fraction are in triples or higher order systems (Tokovinin et al. 2006; Rucinski, Pribulla & van Kerkwijk 2007; Raghavan et al. 2010; Rappaport et al. 2013), potential stellar mergers may serve as keys to the binary fate. On the other hand, as orbital variations are common in contact binaries, the orbital period decay at a high rate induced by a third star proved to be crucial in the case of the recently claimed red nova precursor KIC 9832227 (Molnar et al. 2017) after the revision of its period variations (Socia et al. 2018; Kovacs, Hartman & Bakos 2019).

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Yang & Qian (2015) presented the first compilation of low mass ratio systems (LMRs) with high fill-out factor, and since then many systems have been detected (for reviews, see Qian et al. 2020; Gazeas et al. 2021b). Ongoing all-sky surveys have significantly increased the number of known systems with extreme low mass ratio (LMR), and many more will be discovered in the Rubin Observatory’s Legacy Survey of Space and Time (LSST) era (Ivezić et al. 2019).

This work focuses on the Catalina Sky Survey (CSS) and presents 30 new LMRs with total eclipses. In Section 2, we briefly describe the CSS sample and our method for identifying LMRs. In Section 3, we describe the photometric analysis of the CSS light curves (LCs) and the physical parameters determination. The methods for estimating the absolute parameters in absence of spectroscopic data are also discussed. Our results are presented in Section 4, where the possibility that they may be merger candidates is also discussed. Our final conclusions are summarized in Section 5.

## 2 SAMPLE SELECTION

### 2.1 The Catalina sample

Our sample is selected from the Catalina Real-Time Transient Survey Data Release 2 (CRTS DR2; Drake et al. 2014a), which includes observations spanning 9 yr (2004–2013). CRTS searches for optical transients by using the three CSS telescopes that search for rapidly moving near-Earth objects. CSS covers the sky between declinations  $\delta = -75^\circ$  to  $+65^\circ$ , avoiding crowded regions near the Galactic plane (Drake et al. 2009). The observations were obtained unfiltered in order to maximize the throughput, and then the magnitudes were transformed to an approximate  $V$  magnitude ( $V_{\text{CSS}}$ ; Drake et al. 2014a).

Drake et al. (2014b) investigated the properties of 367 ultrashort-period binary candidates identified from CSS data. Papageorgiou et al. (2018) reported an updated catalogue of 4683 eclipsing Algol-type binaries (EA) from the CSS survey. The physical parameters of the EA systems were explored by Lee (2015), Papageorgiou et al. (2019), and Carmo et al. (2020). Using the same sample of 4683 EA in CSS, Papageorgiou et al. (2021) reported 126 EAs with possible quadratic or cyclic period variations. We focus on the initial sample of Drake et al. (2014a) of 30 743 eclipsing binaries classified as EWs. This sample was explored by Marsh et al. (2017), who characterize 9380 EWs, and more recently by Sun et al. (2020), who presented the physical parameters of 2335 late-type EWs.

### 2.2 Identification of LMRs

Our first step was to exclude from the initial sample systems with insufficiently sampled LCs that have less than 150 observations ( $N_p$ ) and periods longer than  $\sim 0.8$  d, resulting in a sample of 30 592 systems (sample 1). To remove outliers and poor measurements, we first cleaned the LCs of this sample using  $3\sigma$  clipping along the phase-folded LCs, adopting the period from Drake et al. (2014a). Then the initial epoch values were determined using an iterative procedure of fitting a second-degree polynomial to the deeper eclipse. As a result of this procedure, we redetermined the ephemerides of the systems.

As the components of LMRs are characterized by a large difference between their masses, and hence their radii, it is expected that their LCs should exhibit flat bottoms of long duration, compared to common EWs. Since the main idea was to take advantage of the LC morphology, we compiled the LCs of 42 well-studied LMRs from the literature (sample 2) on the basis of their mass ratios, the totality of the eclipses, and the availability of their  $V$ -band LCs.

These are indicated in Table A1 with ‘\*’. For 26 systems from sample 2 that are also identified as extreme LMRs by Şenavcı et al. (2016), the LCs from the *Kepler* mission (Koch et al. 2010) were used. Although *Kepler*’s  $K_p$  filter is essentially a broad VR, its high-accuracy photometry provides valuable information for studies of the LC morphology.

We performed Fourier decomposition (FD) of the phase-folded, normalized flux LCs of both samples, based on the following equation (e.g. Deb & Singh 2009):

$$m(t) = A_0 + \sum_{j=1}^{10} \{a_j \sin[2\pi j\phi(t)] + b_j \cos[2\pi j\phi(t)]\}, \quad (1)$$

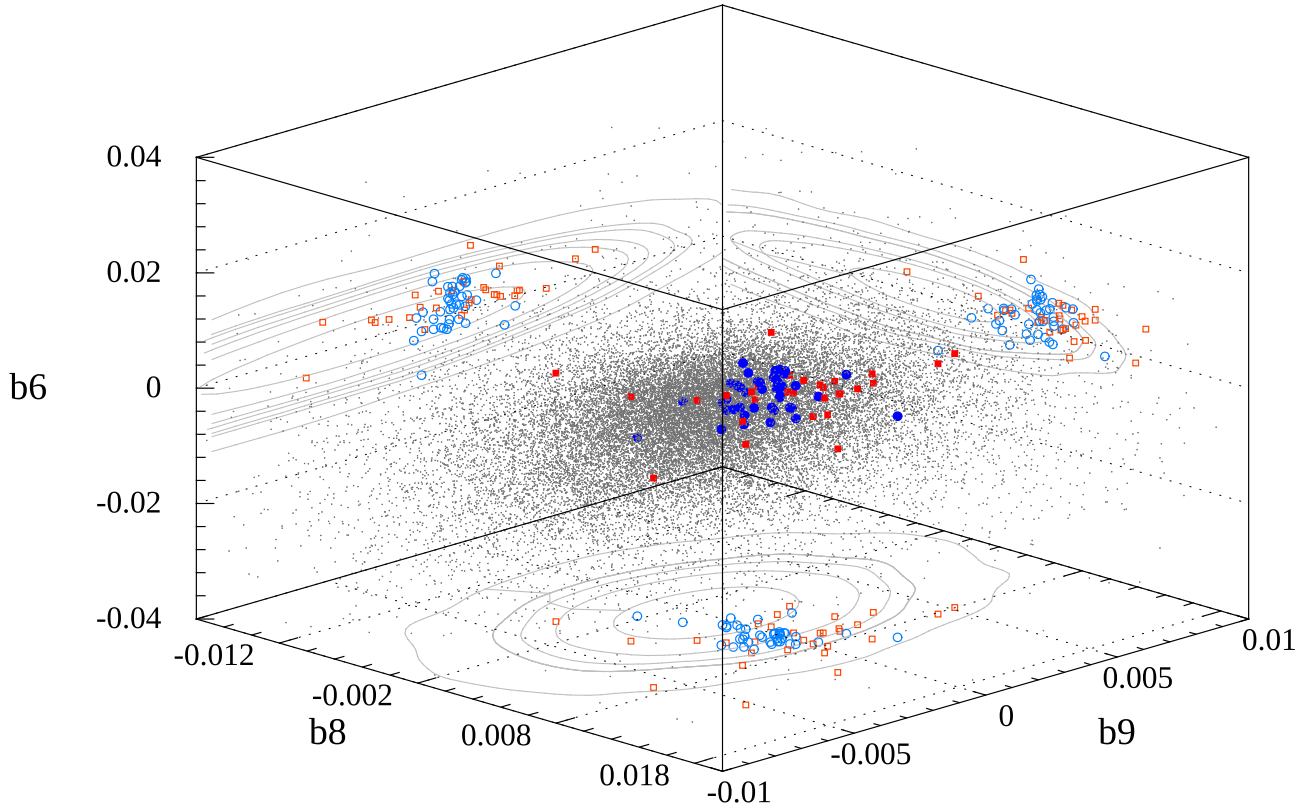
where  $m(t)$  is the observed magnitude at time  $t$ ,  $A_0$  is the mean magnitude,  $a_j$ ,  $b_j$  are the amplitude components of the  $(j - 1)$ th harmonic, and  $\phi(t)$  is the phase (in the range [0–1]) corresponding to a full cycle, with the zero-point of the phased LC corresponding to the primary (deeper) minimum. As to the number of terms to be used in the FD, we choose a high order because otherwise the flat part of the total eclipse cannot be properly reproduced.

We analysed the full set of  $a_j$ ,  $b_j$  coefficients (20 in total), and arrived at the conclusion that the higher order coefficients, especially  $b_8$ , are more efficient in identifying LMRs than are the lower order ones. This can be appreciated from Fig. 1, which shows the distribution of the  $b_6$ ,  $b_8$ , and  $b_9$  coefficients, and where the literature and new candidate LMRs (blue solid circles and red solid squares, respectively) occupy a separate position from the other EWs (grey points). After this analysis, sample 1 was reduced to 2101 candidates. The LCs of the stars in this sample were then subjected to visual inspection, focusing on the totality and duration of the eclipses, finally leading to our sample of 30 new LMR candidates. Table 1 lists the coordinates (RA and Dec), reference time of minimum (in Heliocentric Julian Day, HJD<sub>0</sub>), period ( $P$ ), the CSS magnitude at maximum light ( $V_{\text{CSS}}(\text{max})$ ), the mean photometric error ( $\sigma_{\text{CSS}}$ ), and the number of available CSS observations ( $N_p$ ) of the 30 new CSS LMRs. The overestimated original CSS photometric errors were corrected by using the correction factor provided by Graham et al. (2017), based on the analytical expression derived by Papageorgiou et al. (2018, their footnote 8).

## 3 LIGHT-CURVE MODELLING

The photometric data of the 30 CSS LMR candidates were analysed using PHOEBE-scripser (Prša & Zwitter 2005) to determine the systems’ physical parameters. In the absence of spectroscopic data (as it is often the case for relatively dim,  $V > 13$  mag, EWs), the totality provides the most reliable photometric value for the mass ratio (Terrell & Wilson 2005; Hambálek & Pribulla 2013; Şenavcı et al. 2016). This is usually performed by initializing a 2D grid search on the mass ratio ( $q$ )–inclination ( $i$ ) plane, setting ‘overcontact not in thermal contact’ mode where  $q = M_2/M_1$  is the mass ratio of the system.<sup>1</sup> As we wanted to explore the systems parameter space of the solutions and investigate how well the area of global minimum is mapped in the case of LMRs given the photometry cadence and precision of CSS survey, a synthetic light curve (LC) of a LMR system ( $q = 0.096$ ,  $i = 81.4^\circ$ ) was generated using PHOEBE-scripser. The LC mimics the observational data of CSS having 350 data points and photometric errors around 0.01 mag. The synthetic LC (red

<sup>1</sup>Throughout this work we use number 1 (2) for the more (less) massive component, which is considered to be the primary (secondary).



**Figure 1.** A 3D plot of  $b_6$ ,  $b_8$ , and  $b_9$  FD coefficients of sample 1 EWs represented by grey points and sample 2 (systems from literature, see text for description) represented by solid blue circles. The new CSS candidates (solid red squares) are located on the right top. Contour lines represent the projected distribution of EWs in each plane, while the light blue open circles and light red open squares are the projections of the literature and new LMR systems, respectively.

points) with the photometric errors and the solution (blue line) are shown in Fig. 2 (top panel), whereas the bottom panel of Fig. 2 represents the 2D distribution of  $\log \chi^2$  values in the  $(q, \sin i)$  plane. The solution  $(q_{\min}, i_{\min})$ , as it emerges from the  $q-i$  scan, is  $(0.1, 83^\circ)$ , which is in very good agreement with the real solution of the synthetic system, thus confirming the applicability of the method on this sample.

Following the results of the above test, for a rough estimation of the solution  $(q_{\min}, i_{\min})$ , which was obtained by  $\chi^2$  minimization, the range of explored  $q$  values was set to  $[0.1-0.6]$ , and that of  $i$  values to  $[68^\circ-90^\circ]$ , with step sizes of 0.05 and  $1^\circ$ , respectively. Then, depending on the results, the range was set to  $q_{\min} \pm 0.05$  with a step 0.01 for two runs, one without phase shift and another with phase shift 0.5. During this  $q-i$  scan, the effective temperature of the primary star  $T_1$ , the mass ratio  $q$ , and the orbital inclination  $i$  were set as fixed parameters, while the effective temperature  $T_2$  of the secondary, the modified potential  $\Omega = \Omega_{1,2}$ , and the passband luminosity of the primary  $L_1$  were set as adjustable parameters. Fig. 3 exhibits representative examples of the  $q-i$  scan for four new CSS LMRs.

### 3.1 Initial models for PHOEBE-scripser

To initialize the models, an estimation of the system's temperature is needed since the LC morphology can only constrain the ratio of the components' temperatures ( $T_2/T_1$ ). The effective temperature of the primary was fixed at the system's value ( $T_{\text{sys}}$ ) given by Stassun et al. (2019). This was derived from either spectroscopy or from empirical relations between  $T_{\text{eff}}$  and the *Gaia*  $G_{\text{BP}} - G_{\text{RP}}$  colour

(DR2; Gaia Collaboration et al. 2018), based on a set of 19962 stars having spectroscopically determined  $T_{\text{eff}}$  and being within 100 pc so as to avoid reddening. Taking into account that  $T_{\text{sys}}$  is dominated by the temperature of the primary (hotter) component, we set  $T_{\text{sys}} = T_1$ . Limb-darkening coefficients were interpolated from van Hamme (1993) tables for the given temperatures, while gravity-darkening coefficients  $g$  and surface albedos  $A$  were accordingly assumed for convective ( $g = 0.32, A = 0.5$ ) or radiative envelopes ( $g = 1, A = 1$ ). The synchronization parameters were set as  $F = 1$ , assuming synchronous rotation of the components. Having set the above parameters and before the  $q-i$  scan is performed, the ephemeris of each system was refined by adjusting the reference time of minimum (HJD<sub>0</sub>) in PHOEBE. The resulting values of  $q$  and  $i$ , along with corresponding  $T_2$ ,  $\Omega_{1,2}$ , and  $L_1$  acquired from the fine scan of the parameter space, were used as input parameters to check the solution for each system. The final parameters  $q$ ,  $T_2/T_1$ ,  $\Omega_{1,2}$ ,  $r_1$ ,  $r_2$ ,  $i$ ,  $L_1/L_{\text{tot}}$ , and  $f^2$  are presented in Table 2, where  $r_1, r_2$  are the mean volume radii of the components and  $L_1/L_{\text{tot}}$  is the ratio of the bandpass luminosity of the primary component to the total bandpass luminosity. The LCs of the improved final models are shown in Fig. A1. Four systems (CSS\_J080724.7+164610, CSS\_J082850.5+015641, CSS\_J110526.4+285617, and CSS\_J155637.0+060949) show significant period variation of the order of  $10^{-6} \text{ d yr}^{-1}$  during the 9 yr of CSS data. The third light contribution was also investigated and found to be negligible ( $\leq 1$  per cent) in the context of our photometric

$$^2 f = \frac{\Omega - \Omega_{\text{in}}}{\Omega_{\text{out}} - \Omega_{\text{in}}}, \text{ where } f \text{ is the fill-out factor, and } \Omega_{\text{in}} \text{ and } \Omega_{\text{out}} \text{ are the modified potential of the inner and the outer Lagrangian points, respectively.}$$

**Table 1.** The 30 new LMR candidates selected from sample 1 using Fourier decomposition (FD).

| ID                   | RA <sub>J2000</sub><br>(h:m:s) | Dec <sub>J2000</sub><br>(°:′:″) | HJD <sub>0</sub><br>(245 0000+) | Period<br>(d) | V <sub>CSS(max)</sub><br>(mag) | σ <sub>CSS</sub><br>(mag) | N <sub>p</sub> |
|----------------------|--------------------------------|---------------------------------|---------------------------------|---------------|--------------------------------|---------------------------|----------------|
| CSS_J011848.4+132107 | 01:18:48.49                    | +13:21:07.6                     | 6589.79386                      | 0.3439788     | 13.21                          | 0.01                      | 300            |
| CSS_J015301.5+223638 | 01:53:01.55                    | +22:36:38.4                     | 3653.82712                      | 0.2594140     | 15.92                          | 0.03                      | 274            |
| CSS_J021552.4+324419 | 02:15:52.41                    | +32:44:19.5                     | 5120.91902                      | 0.5737980     | 14.68                          | 0.02                      | 350            |
| CSS_J022044.4+280006 | 02:20:44.42                    | +28:00:06.1                     | 4405.81533                      | 0.7593753     | 14.42                          | 0.02                      | 356            |
| CSS_J030702.2+261521 | 03:07:02.24                    | +26:15:21.8                     | 5648.62161                      | 0.7283894     | 13.98                          | 0.02                      | 374            |
| CSS_J051156.6+011756 | 05:11:56.63                    | +01:17:56.5                     | 3703.75981                      | 0.7527221     | 14.82                          | 0.02                      | 351            |
| CSS_J075839.9+131355 | 07:58:39.98                    | +13:13:55.7                     | 6358.70319                      | 0.4620180     | 14.88                          | 0.02                      | 293            |
| CSS_J075848.2+125656 | 07:58:48.24                    | +12:56:56.1                     | 4922.69449                      | 0.3499800     | 14.08                          | 0.02                      | 293            |
| CSS_J080724.7+164610 | 08:07:24.78                    | +16:46:10.6                     | 5211.84350                      | 0.3629629     | 14.39                          | 0.02                      | 415            |
| CSS_J082140.8+192034 | 08:21:40.85                    | +19:20:34.5                     | 5240.76455                      | 0.4323400     | 15.15                          | 0.02                      | 528            |
| CSS_J082850.5+015641 | 08:28:50.52                    | +01:56:41.1                     | 5301.61530                      | 0.4886486     | 13.37                          | 0.01                      | 346            |
| CSS_J082916.5+131557 | 08:29:16.54                    | +13:15:57.6                     | 5321.64675                      | 0.3729305     | 13.98                          | 0.02                      | 438            |
| CSS_J084222.2+041155 | 08:42:22.24                    | +04:11:55.5                     | 4588.65898                      | 0.2809483     | 15.67                          | 0.03                      | 381            |
| CSS_J093010.1−021624 | 09:30:10.15                    | −02:16:24.9                     | 5240.80316                      | 0.3214746     | 15.56                          | 0.03                      | 318            |
| CSS_J103653.7−072753 | 10:36:53.79                    | −07:27:53.6                     | 5652.74006                      | 0.2444613     | 15.75                          | 0.03                      | 276            |
| CSS_J110526.4+285617 | 11:05:26.44                    | +28:56:17.2                     | 4977.70007                      | 0.3491059     | 14.93                          | 0.02                      | 388            |
| CSS_J112643.3−141735 | 11:26:43.32                    | −14:17:35.7                     | 4537.84328                      | 0.3116524     | 13.60                          | 0.01                      | 156            |
| CSS_J120945.8−025729 | 12:09:45.87                    | −02:57:29.2                     | 5596.86649                      | 0.3114363     | 15.29                          | 0.02                      | 294            |
| CSS_J134010.1+134515 | 13:40:10.17                    | +13:45:15.2                     | 5919.99314                      | 0.4110526     | 14.29                          | 0.02                      | 380            |
| CSS_J134512.0+034251 | 13:45:12.07                    | +03:42:51.1                     | 3762.98614                      | 0.4240236     | 15.22                          | 0.02                      | 349            |
| CSS_J145437.2+060239 | 14:54:37.21                    | +06:02:39.8                     | 4917.95998                      | 0.5436659     | 15.28                          | 0.02                      | 351            |
| CSS_J155637.0+060949 | 15:56:37.09                    | +06:09:49.3                     | 4477.02450                      | 0.3605211     | 15.81                          | 0.03                      | 357            |
| CSS_J161753.6+205014 | 16:17:53.67                    | +20:50:14.1                     | 4954.82770                      | 0.5098331     | 14.60                          | 0.02                      | 379            |
| CSS_J163819.6+034852 | 16:38:19.65                    | +03:48:52.0                     | 6158.79806                      | 0.2053320     | 14.26                          | 0.02                      | 339            |
| CSS_J210300.1+050345 | 21:03:00.14                    | +05:03:45.6                     | 4235.88388                      | 0.5921606     | 13.90                          | 0.01                      | 387            |
| CSS_J211420.2−142710 | 21:14:20.28                    | −14:27:10.8                     | 5530.59888                      | 0.5981238     | 15.32                          | 0.02                      | 297            |
| CSS_J233821.8+200518 | 23:38:21.81                    | +20:05:18.2                     | 6167.79999                      | 0.3545902     | 13.23                          | 0.01                      | 324            |
| CSS_J234145.7+233158 | 23:41:45.73                    | +23:31:58.6                     | 4391.81504                      | 0.5986466     | 13.91                          | 0.01                      | 309            |
| CSS_J234324.8+211100 | 23:43:24.84                    | +21:11:00.4                     | 5585.57623                      | 0.6310680     | 14.50                          | 0.02                      | 332            |
| CSS_J234807.2+193717 | 23:48:07.21                    | +19:37:17.8                     | 5590.60823                      | 0.3800130     | 15.46                          | 0.03                      | 331            |

accuracy in one filter. However in the past, several systems showing low-amplitude LCs on the *Hipparcos* mission (Selam 2004) were later spectroscopically found to be triples and the true mass ratio and/or inclination angle was higher.

### 3.2 Error estimation of the physical parameters

In our analysis we consider that the uncertainty of the mass ratio ( $\delta q$ ) is determined by the step of the grid search, thus we set  $\delta q = 0.010$ . In some cases, the global minimum of the  $\chi^2$  curve is broader and flatter, and so the uncertainty in  $q$  is underestimated. For these systems we consider the values of  $q$  around the global minimum that resulted to  $\chi^2$  increased up to 5 per cent of the minimum value ( $\chi_{\min}^2$ ) and adopt the standard deviation of this area as  $\delta q$ . Thus, for 11 out of 30 systems  $\delta q = 0.010$ , while for the remainder it falls in the range  $0.010 < \delta q \leq 0.025$ . The temperature uncertainty of the systems is taken from Stassun et al. (2019). The uncertainties in the derived physical parameters are estimated by performing Monte Carlo simulations (Papageorgiou & Christopoulou 2015; Papageorgiou et al. 2019), since the formal errors from the fitting of the LC are heavily underestimated. During this procedure, each photometric point of the observed LC was randomly displaced 1000 times according to its photometric error  $\sigma_{\text{CSS}}$ , drawn from a normal distribution with zero mean and  $\sigma_{\text{CSS}}$  as standard deviation. The 1000 synthetic LCs, generated in this way, for each system were then fitted by only adjusting  $T_2$ ,  $\Omega_{1,2}$ ,  $L$ , and  $i$ . We finally extracted the lower and the upper error boundaries from each parameter distribution ( $q$ ,  $T_2/T_1$ ,

$\Omega_{1,2}$ ,  $r_1$ ,  $r_2$ ,  $i$ ,  $L_1/L_{\text{tot}}$ , and  $f$ ). The mean of these is the final error provided for each of these quantities in the final catalogue (Table 2).

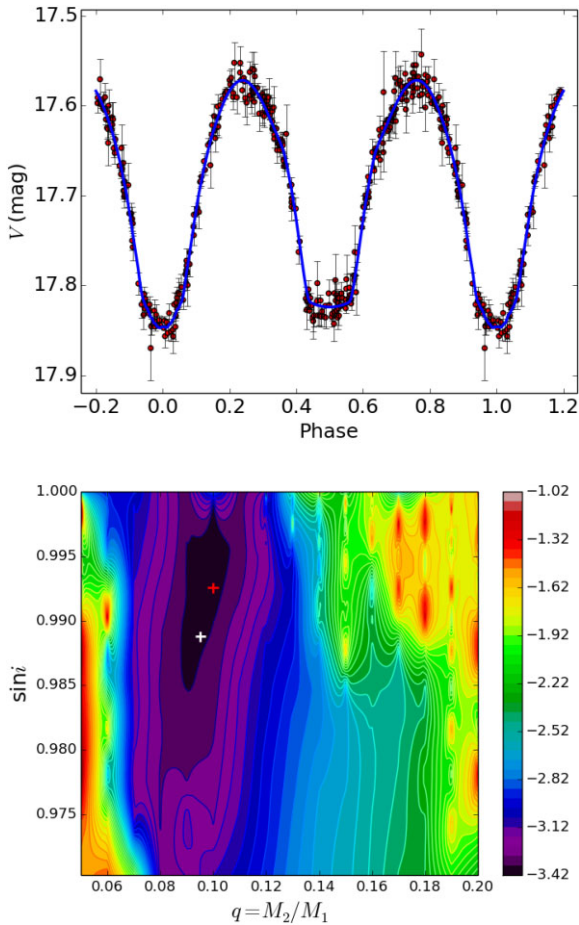
Additionally one of the 30 candidates in our catalogue, namely CSS\_J011848.4+132107 (also known as EM Psc), has already been studied by Yang et al. (2005b), who found, using a V-band LC,  $(q_{\min}, i_{\min}) = (0.100, 83^\circ.3)$ . Qian et al. (2008), using R, I band LCs, later found  $(0.1487, 88^\circ.6)$  for the same system. Our solution,  $(q_{\min}, i_{\min}) = (0.110 \pm 0.015, 89^\circ.6_{-2.2}^{+1.8})$  (see Table 2), is in accordance with Yang et al. (2005b), showing that V<sub>CSS</sub> LCs can be used to estimate the systems' physical parameters.

### 3.3 Absolute parameters

In the absence of spectroscopic data, given the photometric mass ratio of EWs with total eclipses, the usual and simplest way to estimate the primary mass (and consequently  $M_2 = qM_1$ ) and semimajor axis ( $\alpha$ ) is using a spectral type–temperature and spectral type–mass calibration, under the assumption that the primary is on the main sequence (Cox 2000; Pecaute & Mamajek 2013). Other ways include an indirect path of statistically derived relations such as period–mass, period–semimajor axis, or equivalently the total mass of the system (Dimitrov & Kjurkchieva 2015; Yang & Qian 2015; Şenavcı et al. 2016). Another indirect method comes from the published 2D and 3D correlations involving combinations of  $M_1$ ,  $M_2$ ,  $R_1$ ,  $R_2$ ,  $L_1$ ,  $L_2$ ,  $P$ , and  $q$ , as given in Gazeas (2009) based on the data in Gazeas & Stępień (2008).

Alternatively, the absolute parameters of a binary can be estimated out of the absolute magnitude of the primary  $\mathcal{M}_{V1}$ . This can be done





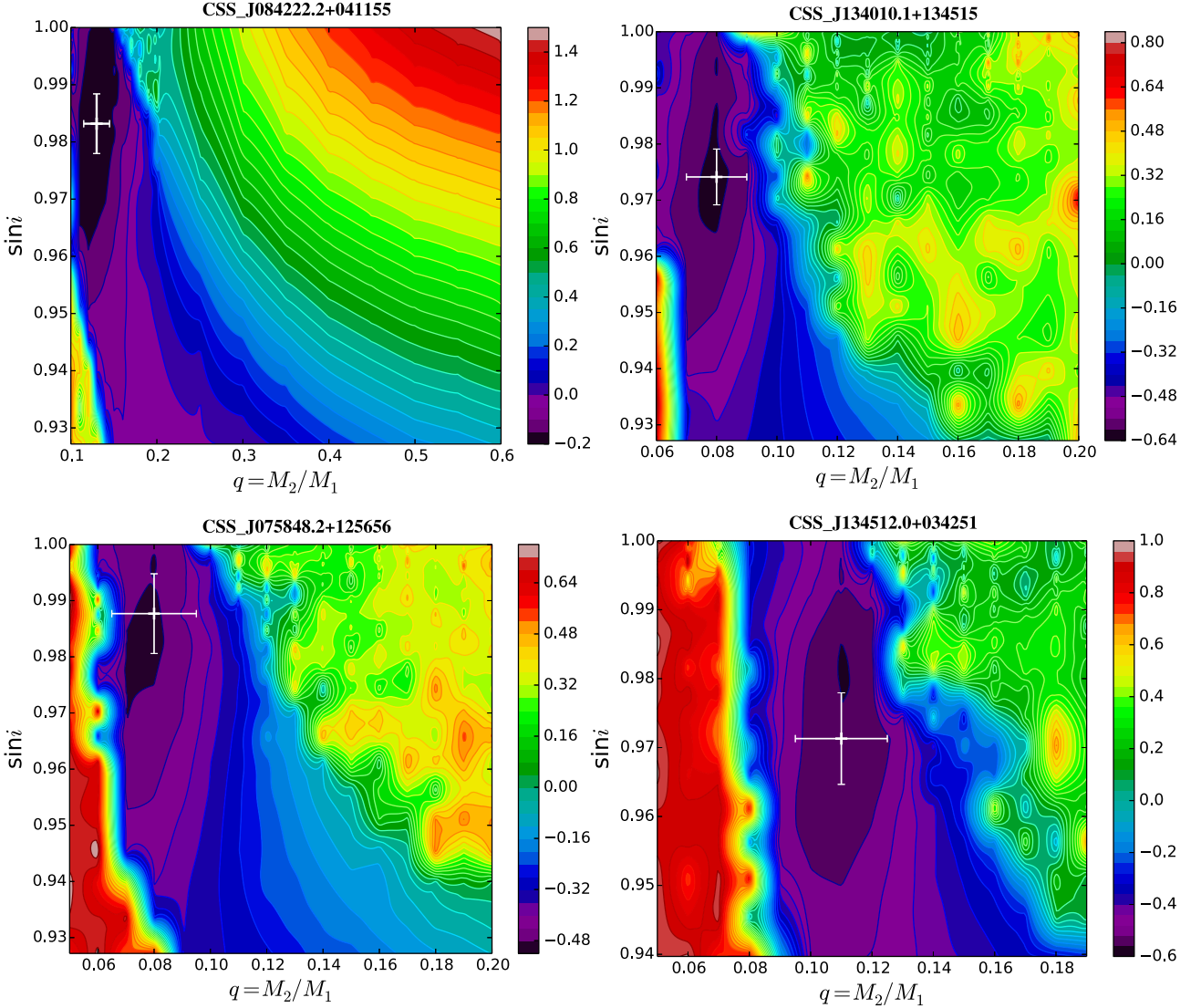
**Figure 2.** Top panel: synthetic LC with photometric errors generated using PHOEBE-scripser (red points). The blue line shows the solution given by our method. Bottom panel: contour plot of  $\log \chi^2$  (colour coded according to the scale on the right) in the  $(q, \sin i)$  plane of the synthetic system. The white cross represents the real solution of the synthetic system, while the red cross represents the resulting solution.

using the passband luminosity ratio of the photometric solution and the maximum magnitude of the system  $\mathcal{M}_{V_{\text{sys}}}$ . The latter can be estimated directly from the data using the *Gaia* distance corrected for the interstellar extinction  $A_V$ . In the case of differential photometry,  $\mathcal{M}_{V_{\text{sys}}}$  can be derived from a period–colour–magnitude relation, such as the one derived by Mateo & Rucinski (2017) based on *Gaia* Data Release 1 (DR1) data (318 EWs) or by Chen et al. (2019) based on *Gaia* DR2 measurements. Next,  $\mathcal{M}_{V_1}$  is converted to  $\mathcal{M}_{\text{bol}}$  based on the bolometric correction (BC) corresponding to the temperature derived from the photometric solution. Finally, the primary mass  $M_1$  is estimated if a mass–luminosity ( $M$ – $L$ ) relation  $L \sim M^\alpha$  is used, under the assumption, well supported by the empirical data, that primary components of contact systems lie in general between the zero-age main sequence (ZAMS) and the terminal-age main sequence (TAMS; Yakut & Eggleton 2005). Sun et al. (2020) used  $\alpha = 4.216$  (Yildiz & Doğan 2013) to infer the mass of the primary. Lu et al. (2020) suggested a method that combined the PADova and TRIeste Stellar Evolution Code (PARSEC; Bressan et al. 2012) with the Roche geometric model to determine the masses of EWs. They applied their method on a sample of 140 spectroscopic studied binaries, and found it to be efficient in high-mass ratio and short-period systems with low effective temperatures.

In this study, we tested all the above methods and empirical relations, as we wanted to select those that provide a better description of the data. For this, we compiled a sample of 161 EWs from Yildiz & Doğan (2013) and Latković, Čeki & Lazarević (2021) with spectroscopically derived mass ratios, since spectroscopic studies are known to produce results with the highest accuracy. This provides us with an extensive and highly heterogeneous sample. We performed a linear fitting in the  $\log M$ – $\log L$  plane of the massive component of this spectroscopic sample. By randomly selecting the mass and luminosity errors from the available literature errors, this fitting was repeated  $10^5$  times. Then, the best pair  $(b, a)$  in the relation  $\log L = \log b + a \log M$  is represented by the mean value of the region where the above fittings have the lowest absolute percentage error (up to 10 per cent) between the calculated and spectroscopic masses. The corresponding uncertainties were derived from the standard deviation of the  $b$  and  $a$  values in the same region. Thus, we derived  $b = 0.63 \pm 0.04$  and  $a = 4.8 \pm 0.2$ . With these values, the above relation predicts the observed masses within  $\Delta M_1 \leq 10$  per cent for 65 per cent of the systems and within  $\Delta M_1 \leq 20$  per cent for 90 per cent of the systems, where  $\Delta M_1 = M_{1,\text{obs}} - M_{1,\text{rel}}$  is the average fractional mass difference,  $M_{1,\text{obs}}$  represents the mass from the analysis of spectroscopic data, and  $M_{1,\text{rel}}$  is the mass obtained from the relation. Nevertheless, we caution that there are several factors that, if not properly accounted for in the analysis, may affect the inferred luminosities of the components, and thereby their masses. This includes, among the others, spots due to magnetic activity, presence of circumstellar material, and third light contributions. In the case of a spotted system, for instance, the inferred luminosities (hence masses) may very well depend on the phase of the magnetic cycle during which the observations are carried out.

We decided to follow the second path and estimate the absolute magnitude of the primary. We cross-matched the LMR sample with *Gaia* Early Data Release 3 (EDR3; Bailer-Jones et al. 2021) using a matching radius of 2 arcsec to find the corresponding distances. The distances of 60 per cent of the sources are  $\leq 2$  kpc. For each source, we also calculate the total line-of-sight Galactic extinction from the 3D dust reddening map of Green et al. (2019), derived from *Gaia* parallaxes and stellar photometry from the Panoramic Survey Telescope and Rapid Response System 1 (Pan-STARRS 1) and the Two Micron All-Sky Survey (2MASS) data. The magnitude of the primary is estimated from the magnitude at quadratures of the system using the results of Table 2 ( $L_1/L_{\text{tot}}$ ). The magnitudes were transformed to Johnson  $V$  based on the relation of Drake et al. (2013). The temperatures of the individual components were derived from disentangling the value of the binary temperature (see Section 3.1) using equation (3) of Zwitter et al. (2003), the ratio of relative radii  $r_2/r_1$  and the temperature ratio  $T_2/T_1$  from the LC analysis (see Table 2). Then the absolute bolometric magnitude is derived based on the bolometric correction (from Bessell, Castelli & Plez 1998) corresponding to the effective temperature of the primary, and the primary luminosity is obtained. Finally, the mass of the primary components was estimated from our derived mass–luminosity relation, and consequently the mass of the secondaries from the mass ratio, the semimajor axis from Kepler’s law, and the mean radii from the corresponding relative radii.

To calculate the uncertainties of the component’s effective temperature ( $\sigma_{T_1}, \sigma_{T_2}$ ), we considered the uncertainty of the systems’ effective temperatures from the *Transiting Exoplanet Survey Satellite* (*TESS*) Input Catalog, v-8.0 (TIC-8) as the dominant source of error, since the temperature ratio  $T_2/T_1$  uncertainty contribution is of the order  $\sim 10$  K, while the ratio of relative radii  $r_2/r_1$  uncertainty contribution is negligible. The remaining uncertainties



**Figure 3.** Contour plots of  $\log \chi^2$  (colour coded according to the scale on the right) in the  $(q, \sin i)$  plane of four CSS LMRs. The white crosses represent the solutions of the systems with the error bars derived from the Monte Carlo procedure.

were calculated considering the photometric error from the LCs, the uncertainty in the  $B - V$  colours (calculated from  $\sigma_B, \sigma_V$ , as given by TIC-8), and the uncertainty of the distance estimation combined with the estimated errors of the physical parameters (Section 3.2). The results are given in Table 3.

#### 4 RESULTS AND DISCUSSION

It can be seen from Table 3 that the new LMRs have mean primary mass  $1.42 \pm 0.26 M_\odot$ , and mean secondary mass  $0.177 \pm 0.048 M_\odot$ . Half of the systems have temperatures in the range 5000–6500 K, while the hottest reaches 7280 K, and there is no preference between A or W subtypes. There are five systems with temperature difference between the components ( $\Delta T$ ) above 500 K, with the mean being about 260 K. We also find no trend in which  $\Delta T$  increases with increasing temperature or with decreasing fill-out factor.

The evolutionary status of these new CSS LMRs can be compared in the mass–radius plane with 173 LMRs compiled from the literature having  $q \leq 0.25$  derived spectroscopically or/and having total eclipse (listed in Table A1). The main source of Table A1 comes from

Latković et al. (2021), but we have excluded systems that have unreliable or peculiarly large or small masses, corrected or updated the absolute parameters of others, and also included new systems. We also did not include LMRs from the automated modelling of Sun et al. (2020) and Li, Liu & Zhang (2020), as we wanted to focus on dedicated studies of LMRs. Fig. 4 shows their location in the  $\log M - \log R$  diagram together with ZAMS and TAMS loci calculated for solar metallicity using the Binary Star Evolution (BSE) code (Hurley, Tout & Pols 2002). The primary and secondary components are gathered in two different areas, above ZAMS and TAMS, respectively, indicating their different status but also their difference with the main-sequence stars of the same mass.

It can be seen from Table 2 that  $\sim 40$  per cent of the 30 new LMRs are deep contact ( $f \geq 50$  per cent) with  $q \leq 0.25$ , and that eight of them, within the errors, belong to the class of extreme LMRs with  $q \leq 0.1$ . Thus, with our 17 new discoveries, there are 43 extreme LMRs, only six of which have spectroscopic mass ratios (listed in Table A1). The latter include the peculiar AW UMa, which shows the largest difference between photometric and spectroscopic mass ratio,  $q = 0.076$  (Eaton 2016) and  $q = 0.099$  (Rucinski 2015, 2020),

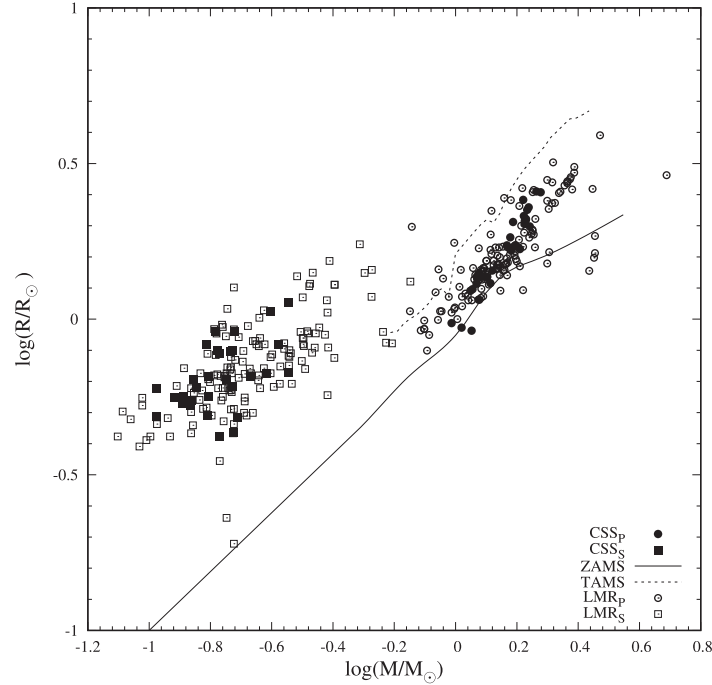
**Table 2.** The physical parameters of the 30 new CSS LMRs derived by LC modelling.

| ID                   | $q$           | $\frac{T_2}{T_1}$ | $\Omega_{12}$ | $r_1$         | $r_2$         | $i$ ( $^\circ$ ) | $\frac{L_1}{L_{\text{tot}}}$ | $f$         |
|----------------------|---------------|-------------------|---------------|---------------|---------------|------------------|------------------------------|-------------|
| CSS_J011848.4+132107 | 0.110 ± 0.015 | 0.975 ± 0.003     | 1.940 ± 0.002 | 0.594 ± 0.001 | 0.237 ± 0.001 | 89.6 ± 2.0       | 0.883                        | 0.68 ± 0.03 |
| CSS_J015301.5+223638 | 0.200 ± 0.015 | 1.026 ± 0.006     | 2.186 ± 0.008 | 0.539 ± 0.003 | 0.269 ± 0.003 | 80.0 ± 1.0       | 0.782                        | 0.36 ± 0.06 |
| CSS_J021552.4+324419 | 0.110 ± 0.010 | 0.920 ± 0.006     | 1.971 ± 0.005 | 0.580 ± 0.002 | 0.221 ± 0.003 | 79.3 ± 2.0       | 0.909                        | 0.25 ± 0.07 |
| CSS_J022044.4+280006 | 0.150 ± 0.010 | 0.944 ± 0.005     | 2.063 ± 0.007 | 0.563 ± 0.003 | 0.249 ± 0.003 | 84.7 ± 1.0       | 0.870                        | 0.41 ± 0.07 |
| CSS_J030702.2+261521 | 0.090 ± 0.015 | 0.952 ± 0.005     | 1.903 ± 0.002 | 0.599 ± 0.001 | 0.213 ± 0.001 | 81.2 ± 0.7       | 0.910                        | 0.42 ± 0.04 |
| CSS_J051156.6+011756 | 0.150 ± 0.010 | 0.925 ± 0.006     | 2.072 ± 0.009 | 0.560 ± 0.004 | 0.245 ± 0.004 | 83.1 ± 2.4       | 0.882                        | 0.32 ± 0.10 |
| CSS_J075839.9+131355 | 0.070 ± 0.010 | 0.869 ± 0.012     | 1.834 ± 0.009 | 0.621 ± 0.004 | 0.203 ± 0.006 | 70.0 ± 2.1       | 0.947                        | 0.61 ± 0.19 |
| CSS_J075848.2+125656 | 0.080 ± 0.015 | 0.974 ± 0.006     | 1.870 ± 0.003 | 0.609 ± 0.002 | 0.207 ± 0.002 | 81.0 ± 2.6       | 0.909                        | 0.48 ± 0.07 |
| CSS_J080724.7+164610 | 0.150 ± 0.015 | 1.006 ± 0.003     | 2.058 ± 0.002 | 0.565 ± 0.001 | 0.251 ± 0.001 | 88.5 ± 1.2       | 0.836                        | 0.46 ± 0.03 |
| CSS_J082140.8+192034 | 0.100 ± 0.010 | 0.966 ± 0.006     | 1.921 ± 0.002 | 0.597 ± 0.001 | 0.226 ± 0.001 | 75.1 ± 1.0       | 0.891                        | 0.59 ± 0.03 |
| CSS_J082850.5+015641 | 0.180 ± 0.015 | 1.001 ± 0.002     | 2.132 ± 0.003 | 0.550 ± 0.001 | 0.265 ± 0.001 | 85.7 ± 0.9       | 0.816                        | 0.44 ± 0.02 |
| CSS_J082916.5+131557 | 0.190 ± 0.010 | 1.037 ± 0.002     | 2.158 ± 0.003 | 0.545 ± 0.001 | 0.267 ± 0.001 | 83.3 ± 1.1       | 0.786                        | 0.41 ± 0.02 |
| CSS_J084222.2+041155 | 0.130 ± 0.015 | 1.016 ± 0.006     | 2.000 ± 0.007 | 0.579 ± 0.003 | 0.245 ± 0.003 | 79.5 ± 1.6       | 0.845                        | 0.56 ± 0.08 |
| CSS_J093010.1-021624 | 0.110 ± 0.020 | 1.031 ± 0.006     | 1.921 ± 0.003 | 0.603 ± 0.001 | 0.249 ± 0.002 | 78.0 ± 2.3       | 0.842                        | 0.96 ± 0.03 |
| CSS_J103653.7-072753 | 0.180 ± 0.010 | 1.070 ± 0.005     | 2.175 ± 0.011 | 0.535 ± 0.004 | 0.246 ± 0.004 | 82.9 ± 2.2       | 0.768                        | 0.06 ± 0.04 |
| CSS_J110526.4+285617 | 0.110 ± 0.015 | 1.031 ± 0.005     | 1.923 ± 0.003 | 0.602 ± 0.001 | 0.248 ± 0.002 | 85.8 ± 2.4       | 0.839                        | 0.93 ± 0.04 |
| CSS_J112643.3-141735 | 0.120 ± 0.020 | 1.033 ± 0.004     | 1.950 ± 0.003 | 0.595 ± 0.001 | 0.253 ± 0.002 | 79.3 ± 1.5       | 0.834                        | 0.88 ± 0.04 |
| CSS_J120945.8-025729 | 0.140 ± 0.015 | 1.073 ± 0.005     | 1.989 ± 0.003 | 0.588 ± 0.001 | 0.270 ± 0.002 | 81.2 ± 2.1       | 0.787                        | 0.95 ± 0.03 |
| CSS_J134010.1+134515 | 0.080 ± 0.010 | 0.964 ± 0.006     | 1.876 ± 0.003 | 0.607 ± 0.001 | 0.204 ± 0.001 | 76.9 ± 1.3       | 0.913                        | 0.37 ± 0.05 |
| CSS_J134512.0+034251 | 0.110 ± 0.015 | 0.966 ± 0.007     | 1.970 ± 0.006 | 0.581 ± 0.003 | 0.221 ± 0.003 | 79.2 ± 1.6       | 0.889                        | 0.27 ± 0.08 |
| CSS_J145437.2+060239 | 0.110 ± 0.010 | 0.914 ± 0.009     | 1.959 ± 0.008 | 0.586 ± 0.003 | 0.227 ± 0.004 | 79.3 ± 1.6       | 0.909                        | 0.43 ± 0.11 |
| CSS_J155637.0+060949 | 0.120 ± 0.025 | 1.033 ± 0.007     | 1.944 ± 0.009 | 0.598 ± 0.002 | 0.257 ± 0.003 | 75.9 ± 1.6       | 0.833                        | 0.96 ± 0.04 |
| CSS_J161753.6+205014 | 0.080 ± 0.010 | 0.980 ± 0.008     | 1.894 ± 0.003 | 0.598 ± 0.001 | 0.193 ± 0.002 | 78.0 ± 1.3       | 0.912                        | 0.04 ± 0.02 |
| CSS_J163819.6+034852 | 0.150 ± 0.015 | 0.999 ± 0.004     | 2.034 ± 0.003 | 0.575 ± 0.001 | 0.263 ± 0.002 | 87.1 ± 1.8       | 0.833                        | 0.71 ± 0.03 |
| CSS_J210300.1+050345 | 0.100 ± 0.015 | 0.912 ± 0.005     | 1.937 ± 0.003 | 0.590 ± 0.001 | 0.217 ± 0.001 | 82.8 ± 1.2       | 0.917                        | 0.34 ± 0.04 |
| CSS_J211420.2-142710 | 0.110 ± 0.020 | 1.126 ± 0.006     | 1.976 ± 0.010 | 0.578 ± 0.004 | 0.218 ± 0.004 | 74.3 ± 1.2       | 0.814                        | 0.18 ± 0.10 |
| CSS_J233821.8+200518 | 0.220 ± 0.015 | 1.003 ± 0.002     | 2.236 ± 0.009 | 0.531 ± 0.003 | 0.275 ± 0.003 | 86.3 ± 2.6       | 0.790                        | 0.33 ± 0.06 |
| CSS_J234145.7+233158 | 0.090 ± 0.015 | 1.000 ± 0.006     | 1.882 ± 0.002 | 0.610 ± 0.001 | 0.226 ± 0.001 | 77.7 ± 0.9       | 0.884                        | 0.78 ± 0.04 |
| CSS_J234324.8+211100 | 0.110 ± 0.010 | 0.994 ± 0.005     | 1.941 ± 0.002 | 0.594 ± 0.001 | 0.237 ± 0.001 | 80.6 ± 1.0       | 0.870                        | 0.68 ± 0.03 |
| CSS_J234807.2+193717 | 0.180 ± 0.020 | 1.044 ± 0.005     | 2.137 ± 0.006 | 0.551 ± 0.002 | 0.265 ± 0.003 | 87.9 ± 1.8       | 0.786                        | 0.40 ± 0.05 |

**Table 3.** The absolute parameters of the 30 new CSS LMRs.

| ID                   | $T_{\text{sys}}$<br>(K) | $T_1$<br>(K) | $T_2$<br>(K) | $M_1$<br>( $M_\odot$ ) | $M_2$<br>( $M_\odot$ ) | $R_1$<br>( $R_\odot$ ) | $R_2$<br>( $R_\odot$ ) | $L_1$<br>( $L_\odot$ ) | $L_2$<br>( $L_\odot$ ) | $\frac{L}{L_\odot}$ | $\left(\frac{L}{L_\odot}\right)_k$ |
|----------------------|-------------------------|--------------|--------------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|---------------------|------------------------------------|
| CSS_J011848.4+132107 | 5723 ± 100              | 5742 ± 101   | 5600 ± 99    | 1.25 ± 0.05            | 0.14 ± 0.02            | 1.37 ± 0.02            | 0.55 ± 0.01            | 1.85 ± 0.34            | 0.26 ± 0.02            | 0.217               | 0.195                              |
| CSS_J015301.5+223638 | 4811 ± 175              | 4786 ± 174   | 4909 ± 180   | 0.97 ± 0.02            | 0.19 ± 0.02            | 0.97 ± 0.01            | 0.48 ± 0.01            | 0.55 ± 0.06            | 0.12 ± 0.02            | 0.110               | 0.171                              |
| CSS_J021552.4+324419 | 6801 ± 176              | 6863 ± 178   | 6315 ± 169   | 1.70 ± 0.07            | 0.19 ± 0.02            | 2.08 ± 0.03            | 0.79 ± 0.01            | 8.03 ± 1.29            | 0.89 ± 0.10            | 0.207               | 0.117                              |
| CSS_J022044.4+280006 | 6702 ± 229              | 6760 ± 231   | 6382 ± 220   | 1.89 ± 0.09            | 0.28 ± 0.02            | 2.56 ± 0.04            | 1.13 ± 0.02            | 13.64 ± 2.37           | 1.90 ± 0.27            | 0.150               | 0.092                              |
| CSS_J030702.2+261521 | 6646 ± 63               | 6680 ± 63    | 6362 ± 70    | 1.84 ± 0.07            | 0.17 ± 0.03            | 2.57 ± 0.03            | 0.91 ± 0.01            | 11.72 ± 1.62           | 1.23 ± 0.06            | 0.264               | 0.148                              |
| CSS_J051156.6+011756 | 6344 ± 156              | 6414 ± 158   | 5936 ± 152   | 1.73 ± 0.08            | 0.26 ± 0.02            | 2.45 ± 0.04            | 1.07 ± 0.02            | 8.76 ± 1.58            | 1.28 ± 0.14            | 0.148               | 0.089                              |
| CSS_J075839.9+131355 | 6643 ± 138              | 6714 ± 140   | 5833 ± 145   | 1.51 ± 0.06            | 0.11 ± 0.02            | 1.83 ± 0.03            | 0.60 ± 0.02            | 4.57 ± 0.70            | 0.37 ± 0.04            | 0.356               | 0.187                              |
| CSS_J075848.2+125656 | 6095 ± 25               | 6111 ± 25    | 5951 ± 41    | 1.32 ± 0.04            | 0.11 ± 0.02            | 1.43 ± 0.01            | 0.49 ± 0.01            | 2.39 ± 0.24            | 0.27 ± 0.01            | 0.303               | 0.229                              |
| CSS_J080724.7+164610 | 5991 ± 22               | 5984 ± 22    | 6022 ± 31    | 1.25 ± 0.03            | 0.19 ± 0.02            | 1.37 ± 0.01            | 0.61 ± 0.01            | 1.86 ± 0.20            | 0.44 ± 0.01            | 0.151               | 0.140                              |
| CSS_J082140.8+192034 | 7097 ± 158              | 7126 ± 159   | 6882 ± 159   | 1.56 ± 0.07            | 0.16 ± 0.02            | 1.72 ± 0.02            | 0.65 ± 0.01            | 5.38 ± 0.94            | 0.86 ± 0.08            | 0.239               | 0.131                              |
| CSS_J082850.5+015641 | 6428 ± 35               | 6426 ± 35    | 6433 ± 38    | 1.47 ± 0.05            | 0.26 ± 0.02            | 1.73 ± 0.02            | 0.83 ± 0.01            | 4.04 ± 0.45            | 1.06 ± 0.03            | 0.124               | 0.076                              |
| CSS_J082916.5+131557 | 6051 ± 24               | 6006 ± 24    | 6226 ± 28    | 1.27 ± 0.04            | 0.24 ± 0.01            | 1.36 ± 0.01            | 0.67 ± 0.01            | 1.98 ± 0.26            | 0.60 ± 0.02            | 0.117               | 0.109                              |
| CSS_J084222.2+041155 | 6325 ± 168              | 6310 ± 168   | 6408 ± 174   | 1.19 ± 0.05            | 0.16 ± 0.02            | 1.15 ± 0.02            | 0.49 ± 0.01            | 1.49 ± 0.27            | 0.36 ± 0.04            | 0.179               | 0.181                              |
| CSS_J093010.1-021624 | 5746 ± 224              | 5720 ± 223   | 5894 ± 232   | 1.17 ± 0.04            | 0.13 ± 0.02            | 1.30 ± 0.02            | 0.54 ± 0.01            | 1.35 ± 0.22            | 0.31 ± 0.05            | 0.224               | 0.236                              |
| CSS_J103653.7-072753 | 5446 ± 227              | 5487 ± 229   | 5287 ± 222   | 1.05 ± 0.04            | 0.19 ± 0.01            | 0.94 ± 0.01            | 0.43 ± 0.01            | 0.74 ± 0.14            | 0.13 ± 0.02            | 0.117               | 0.159                              |
| CSS_J110526.4+285617 | 5297 ± 210              | 5273 ± 209   | 5435 ± 216   | 1.17 ± 0.06            | 0.13 ± 0.02            | 1.37 ± 0.02            | 0.57 ± 0.01            | 1.37 ± 0.32            | 0.25 ± 0.04            | 0.224               | 0.234                              |
| CSS_J112643.3-141735 | 5557 ± 148              | 5528 ± 147   | 5709 ± 153   | 1.14 ± 0.03            | 0.14 ± 0.02            | 1.25 ± 0.01            | 0.53 ± 0.01            | 1.17 ± 0.11            | 0.27 ± 0.03            | 0.203               | 0.229                              |
| CSS_J120945.8-025729 | 5640 ± 159              | 5563 ± 157   | 5967 ± 171   | 1.12 ± 0.05            | 0.16 ± 0.01            | 1.23 ± 0.02            | 0.57 ± 0.01            | 1.09 ± 0.21            | 0.36 ± 0.04            | 0.174               | 0.206                              |
| CSS_J134010.1+134515 | 6924 ± 35               | 6949 ± 36    | 6695 ± 53    | 1.52 ± 0.06            | 0.12 ± 0.02            | 1.66 ± 0.02            | 0.56 ± 0.01            | 4.71 ± 0.70            | 0.56 ± 0.02            | 0.301               | 0.159                              |
| CSS_J134512.0+034251 | 7006 ± 188              | 7035 ± 189   | 6797 ± 190   | 1.62 ± 0.07            | 0.18 ± 0.03            | 1.68 ± 0.02            | 0.64 ± 0.01            | 6.47 ± 1.06            | 0.78 ± 0.09            | 0.208               | 0.116                              |
| CSS_J145437.2+060239 | 6861 ± 192              | 6930 ± 194   | 6336 ± 189   | 1.68 ± 0.10            | 0.18 ± 0.02            | 2.02 ± 0.04            | 0.78 ± 0.02            | 7.65 ± 1.98            | 0.89 ± 0.12            | 0.211               | 0.119                              |
| CSS_J155637.0+060949 | 6343 ± 168              | 6309 ± 167   | 6516 ± 178   | 1.26 ± 0.06            | 0.15 ± 0.03            | 1.43 ± 0.02            | 0.61 ± 0.01            | 1.93 ± 0.37            | 0.61 ± 0.07            | 0.205               | 0.182                              |
| CSS_J161753.6+205014 | 6993 ± 22               | 7006 ± 22    | 6864 ± 66    | 1.75 ± 0.06            | 0.14 ± 0.02            | 1.99 ± 0.02            | 0.64 ± 0.01            | 9.22 ± 1.04            | 0.82 ± 0.04            | 0.292               | 0.160                              |
| CSS_J163819.6+034852 | 6662 ± 162              | 6665 ± 162   | 6649 ± 164   | 1.13 ± 0.03            | 0.17 ± 0.02            | 0.92 ± 0.01            | 0.42 ± 0.00            | 1.13 ± 0.10            | 0.31 ± 0.03            | 0.157               | 0.183                              |
| CSS_J210300.1+050345 | 6723 ± 143              | 6787 ± 144   | 6188 ± 136   | 1.67 ± 0.05            | 0.17 ± 0.03            | 2.15 ± 0.02            | 0.79 ± 0.01            | 7.46 ± 0.58            | 0.82 ± 0.07            | 0.233               | 0.129                              |
| CSS_J211420.2-142710 | 6778 ± 164              | 6876 ± 166   | 6171 ± 157   | 1.51 ± 0.09            | 0.17 ± 0.03            | 2.05 ± 0.04            | 0.77 ± 0.02            | 4.59 ± 1.31            | 0.78 ± 0.09            | 0.206               | 0.112                              |
| CSS_J233821.8+200518 | 5991 ± 175              | 5987 ± 175   | 6006 ± 176   | 1.30 ± 0.04            | 0.29 ± 0.02            | 1.30 ± 0.01            | 0.68 ± 0.01            | 2.23 ± 0.28            | 0.53 ± 0.06            | 0.099               | 0.090                              |
| CSS_J234145.7+233158 | 6853 ± 151              | 6853 ± 151   | 6852 ± 155   | 1.71 ± 0.05            | 0.15 ± 0.03            | 2.24 ± 0.02            | 0.83 ± 0.01            | 8.39 ± 0.69            | 1.37 ± 0.13            | 0.273               | 0.152                              |
| CSS_J234324.8+211100 | 6635 ± 152              | 6640 ± 152   | 6603 ± 155   | 1.73 ± 0.06            | 0.19 ± 0.02            | 2.29 ± 0.03            | 0.91 ± 0.01            | 8.86 ± 1.10            | 1.42 ± 0.14            | 0.217               | 0.124                              |
| CSS_J234807.2+193717 | 5553 ± 164              | 5504 ± 163   | 5749 ± 172   | 1.19 ± 0.04            | 0.21 ± 0.03            | 1.36 ± 0.02            | 0.66 ± 0.01            | 1.45 ± 0.24            | 0.42 ± 0.05            | 0.125               | 0.133                              |





**Figure 4.** The primary and secondary components of CSS LMRs (solid circles and solid squares, respectively), combined with primary and secondary components from previous LMRs from the literature (open circles and open squares, respectively), plotted on the  $\log M$ – $\log R$  diagram. Zero-age main sequence (ZAMS; solid) and terminal-age main sequence (TAMS; dotted) lines at solar metallicity, as obtained using the BSE code (Hurley et al. 2002), are overplotted.

respectively. The remaining five systems are SX CrV, V870 Ara, KR Com, FP Boo, and XX Sex. The system with the highest fill-out factor ( $f \sim 99$  per cent) is KR Com, which also has a large third light contribution at the level of 60 per cent, while SX CrV is the system with the lowest fill-out factor ( $f \sim 27$  per cent). As can be seen in Fig. 5, where all previously known LMRs are plotted together with EWs with spectroscopic mass ratio ( $EW_{sp}$ ) and new CSS LMRs, the smallest the  $q$  value, the larger the fill-out factor distribution range. It is obvious that in previous LMRs that have both total eclipses and spectroscopic mass ratio, the symbols coincide.

#### 4.1 Pre-merger candidates

According to Hut (1980), a binary system becomes unstable if the ratio of the sum of the spin angular momenta of the stars ( $J_s$ ) to the orbital angular momentum ( $J_o$ ) exceeds  $\sim 1/3$  (Darwin’s instability), and is heading towards merging because the companion star can no longer keep the primary star synchronously rotating via the tidal interaction.

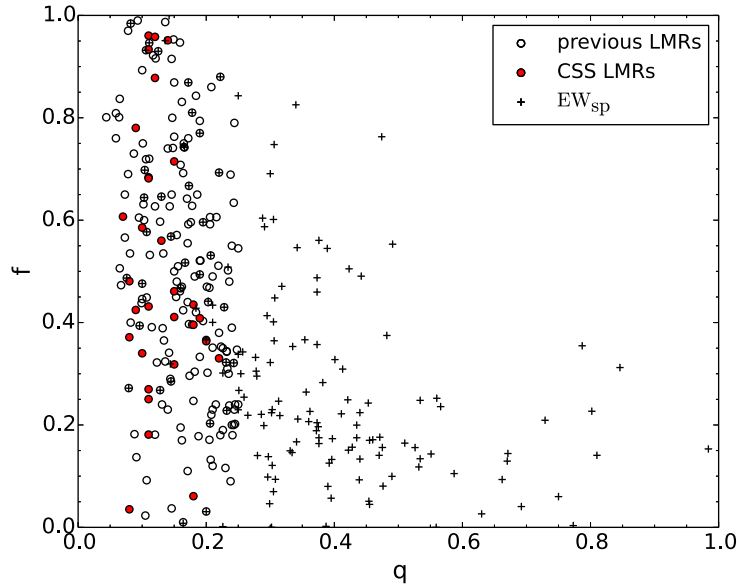
To investigate the stability of the 30 new LMRs listed in Tables 1–3, we determine this ratio using the formula derived from equations (1) and (2) of Li & Zhang (2006):

$$\frac{J_s}{J_o} = \frac{(1+q)}{q} (k_1 r_1)^2 \left[ 1 + q \left( \frac{k_2}{k_1} \right)^2 \left( \frac{r_2}{r_1} \right)^2 \right], \quad (2)$$

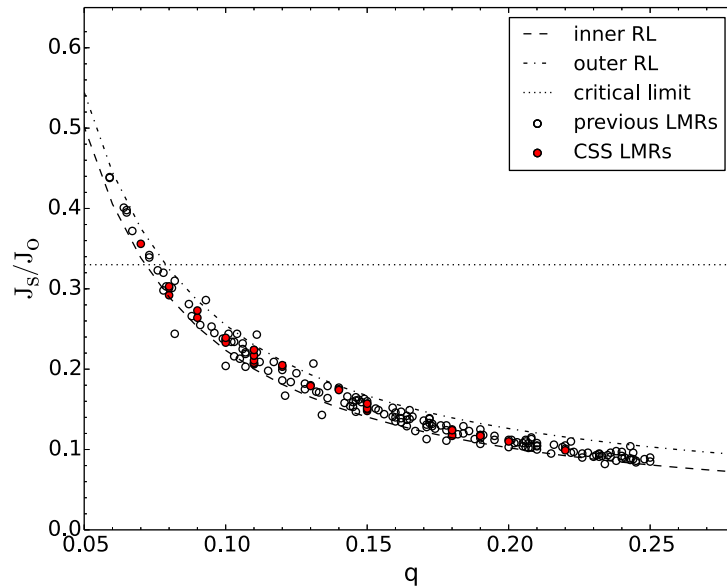
where  $q$  is the mass ratio of the system and  $k_1, k_2$  are the dimensionless gyration radii of both components. The estimation of the gyration radii is crucial for the above estimation even when the mass ratio of the system is known spectroscopically, since it depends on the internal structure of the star. Main-sequence stars tend to have gyration radii from 0.075 (fully radiative) to 0.205 (fully convective). Assuming  $k_1^2 = k_2^2 = k^2 = 0.06$  (Sun like) as in Rasio (1995) and Li & Zhang (2006), the results for the 30 new LMRs are plotted in Fig. 6.

It is seen in Fig. 6 and in Tables 3 and A1 that the majority of the systems lies in the region limited between the inner and outer Roche lobes. Nevertheless, CSS\_J075839.9+131355, V1187 Her, V857 Her, ASAS 083241+2332, V53 (in the globular cluster M4 = NGC 6121), and six contact binaries from *Kepler* Input Catalog (KIC; KIC 4244929, KIC 9151972, KIC 11097678, KIC 8539720, KIC 3127873, and KIC 12352712) are in the instability area, i.e. have surpassed the  $J_s/J_o = 1/3$  limit, and accordingly should have already merged. Alternative solutions that take into account phase smearing, as proposed by Zola et al. (2017), may be possible for the KICs. Three of them with periods  $P > 0.67$  d may have different  $q, i$  model when third light is included in the *Kepler* LC with binned data. V53 is a member of the globular cluster M4, and a blue straggler with a decreasing period (Kaluzny, Thompson & Krzeminski 1997; Li et al. 2017). We therefore reestimate the ratio  $\frac{J_s}{J_o}$  assuming  $k_1^2 \neq k_2^2$  using the tabulated results of Landin, Mendes & Vaz (2009), which take into account the combined effects of tidal and rotational distortions on a star in a binary system. For different masses of the primary components in the ZAMS, we calculate  $k_1^2$  from the linear relationships, we derived as  $k_1 = -0.250 M + 0.539$  for stars with  $M = 0.5$ – $1.4 M_\odot$  and  $k_1 = 0.014 M + 0.152$  for stars with  $M > 1.4 M_\odot$ , although in this range it can be considered approximately constant with a value of  $k_1 \approx 0.18$ . Jiang et al. (2010) also found that  $k^2$  decreases with increasing mass and age of the star if the star’s mass is less than about  $1.3 M_\odot$ , and that above this mass  $k^2$  is roughly constant. For the secondary we assume  $k_2^2 \sim 0.205$ , in accordance with a fully convective star (Arbutina 2007), which is a good assumption as it is a very low mass star ( $M_2 < 0.3 M_\odot$ ), although we know that it is oversized compared to a main-sequence star of the same mass due to energy transfer. The results of the angular momentum ratio against the mass ratio  $q$  assuming different values of gyration radius for the two components are presented in Fig. 7.





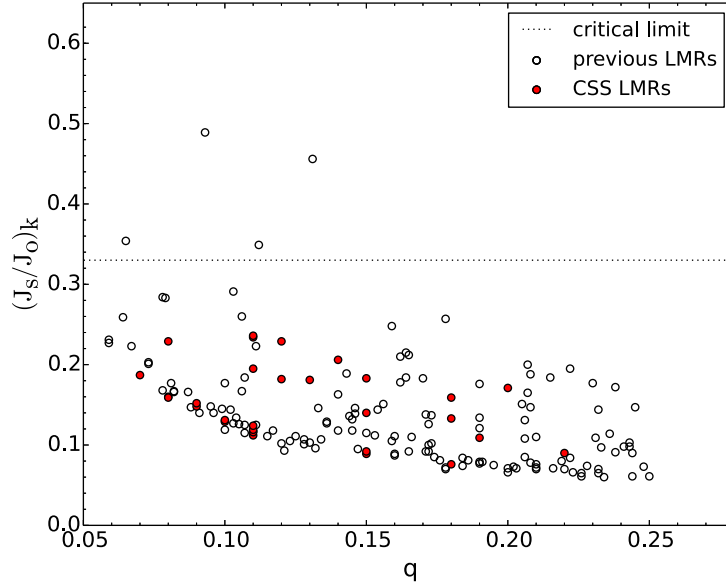
**Figure 5.** The relation  $q$ - $f$  for all previous LMRs (open circles) from Table A1, new CSS LMRs (solid red circles), and EWs with spectroscopically derived mass ratios ( $EW_{sp}$ , crosses). In previous LMRs having both total eclipses and spectroscopic mass ratio, the symbols coincide.



**Figure 6.** The angular momentum ratio  $\frac{J_s}{J_0}$  against the mass ratio  $q$  assuming  $k^2 = 0.06$  for both components of all previous LMRs (open circles) from Table A1 and new CSS LMRs (solid red circles). The dashed and dashed–dotted lines correspond to theoretical systems filling the inner and outer Roche lobes, respectively, and the dotted line to the instability limit  $\frac{J_s}{J_0} = 0.33$ .

As seen from Fig. 7 and Tables 3 and A1, the scatter is larger than Fig. 6 but the majority of the LMRs has not surpassed the dynamical stability limit, with the exceptions of KR Com (0.489), ASAS J102556+2049.3 (0.456), ASAS J083241+2332.4 (0.354), and V1222 Tau (0.349), that should have already merged. Although these systems have different fill-out factors (99 per cent, 24 per cent, 51–70 per cent, and 53 per cent, respectively) and primary masses, all of them show indications of the presence of a third body. ASAS J102556+2049.3 has a large period decrease over 11 yr ( $dP/dt = -3.4 \times 10^{-6} \text{ d yr}^{-1}$ ; Kjurkchieva, Popov & Petrov 2019b), ASAS J083241+2332.4 shows a sinusoidal period variation (Sriram et al. 2016), the spectroscopically studied KR Com has a

third light contribution at the level of 60 per cent (Gazeas et al. 2021a), and V1222 Tau has one of the largest period variations  $dP/dt = +8.19 \times 10^{-6} \text{ d yr}^{-1}$  and an extreme O’Connell effect. Like in many LMRs, the long term period variations are associated with the presence of an additional component (Pribulla & Rucinski 2006) that plays a particular role in angular momentum evolution (Eggleton & Kisseleva-Eggleton 2006). Some information on the possible triplicity could be obtained from the so-called astrometric overnoise parameter renormalized unit weight error (RUWE) in the *Gaia* EDR3 (Stassun & Torres 2021). This is an indicator for the multiplicity of a source when  $\geq 1.4$ , although according to Stassun & Torres (2021) RUWE values even slightly greater than 1.0



**Figure 7.** The angular momentum ratio  $\left(\frac{J_s}{J_o}\right)_k$  against the mass ratio  $q$  assuming different values of  $k_1^2$  for the massive component and  $k_2^2 \sim 0.205$  for the less massive component. The symbols are as in Fig. 6.

may signify unresolved binaries in *Gaia* EDR3. Only two systems, CSS\_J011848.4+132107 (EM Psc) and CSS\_J233821.8+200518 have RUWE 3.6 and 3.7, respectively, whereas 17 CSS LMRs have slightly greater than 1.0 as it is the case of CSS\_J110526.4+285617 (1.112) and CSS\_J155637.0+060949 (1.024) that have also large orbital period variation. However, *Gaia* is insensitive to short-period triples and systems where photocentre does not move significantly (see fig. 4 in Belokurov et al. 2020). This is the case of systems detected by *TESS* with RUWE  $\leq 1.4$  like TIC 388459317 (0.952), TIC 52041148 (1.052) (Borkovits et al. 2022), or even quadruples like TIC 278956474 (1.06; Rowden et al. 2020) where the low RUWE value suggests the two binaries are likely to be tightly bound.

Nevertheless, the uncertainty in the determination of the mass of the primary component, and consequently  $k_1$ , determines the uncertainty of the  $\frac{J_s}{J_o}$  ratio. Under the assumption that the primary is a typical main-sequence star with an effective temperature of e.g. 5880–5440 K, corresponding to spectral types G0–G8, a mass uncertainty of 16 per cent results to an uncertainty of  $\pm 24$  per cent of the  $\frac{J_s}{J_o}$  ratio. Thus, we consider additionally as potential pre-mergers, systems with  $\left(\frac{J_s}{J_o}\right)_k \sim 0.3$ , like ZZ PsA, SX CrV, and ASAS J165139+2255.7. For ZZ PsA, our result is consistent with the recent study of Wadhwa et al. (2021b), who characterized ZZ PsA as a bright nova progenitor by developing a new relationship among the mass of the primary, the instability mass ratio  $q_{\text{inst}}$ , and the degree of contact. Following their methodology, we estimated for V1222 Tau, SX CrV, and ASAS J165139+2255.7 the ratio of the reported photometric mass ratio to the instability mass ratio  $q/q_{\text{inst}}$  to be 0.89, 1.08, and 0.96, respectively, at a separation and period (1.95  $R_\odot$ , 0.3143 d) for V1222 Tau, (0.204  $R_\odot$ , 0.292 d) for SX CrV, and (2.24  $R_\odot$ , 0.363251 d) for ASAS J165139+2255.7, suggesting that these systems will enter an unstable phase. ASAS J083241+2332.4 and KR Com have  $q/q_{\text{inst}} = (0.85, 0.65)$ , as well as theoretical instability separation and period (2.29  $R_\odot$ , 0.3515 d) and (2.763  $R_\odot$ , 0.543028 d), respectively. Among the new CSS LMRs, CSS\_J075848.2+125656, with  $q/q_{\text{inst}} = 1.23 \pm 0.23$ , and CSS\_J093010.1–021624, with  $q/q_{\text{inst}} = 1.25 \pm 0.23$ , can be considered as merging system candidates.

## 5 CONCLUSIONS

In this paper, we mine and model 30 new totally eclipsing CSS LMRs. We present their physical parameters ( $T_2/T_1$ ,  $R_2/R_1$ ,  $\Omega_{1,2}$ ,  $i$ ,  $f$ ) and the systems' global parameters, as determined from the LC solutions and *Gaia* EDR3 distances.

Normally, LMRs should have a deep contact configuration, but the existence also of systems far away from this expected state may indicate different evolutionary states. LMRs presenting a shallow or medium degree of contact may be the result of mass transfer from the less massive to the more massive component, which causes the orbit to enlarge without breaking the contact. In the case of a high contact degree, the surface of the binary is very close to its outer critical Roche lobe, and a long-term period decrease due to mass transfer or angular momentum loss via magnetic braking can cause the orbit to tighten, the inner and outer critical Roche lobes to shrink, and the degree of contact to increase. In the case of a high contact degree with continuous mass transfer from the more massive to the less massive (increasing period), and mass loss from the second Lagrange point ( $L_2$ ), the orbit of the system is contracting, with the mass ratio decreasing, and the evolution ends with a rapidly rotating single star. Tidal friction in the presence of a circumstellar disc or a third (or more) companion(s) can constitute another possible mechanism of angular momentum or mass loss (Tutukov, Dremova & Svechnikov 2004; Martin, Spruit & Tata 2011).

Why do systems with a lower mass ratio than theoretically predicted for stability exist? If the observations do not support the Darwin instability criterion in such systems, maybe the mechanism of merger is a different one, or we need to reconsider the parameters involved. Primarily since the primary's dimensionless gyration radius  $k_1$  depends on the primary's mass  $M_1$ , in the case of a photometric solution with total eclipse,  $M_1$  estimation is based on various assumptions that need to be reexamined. In addition, more realistic calculations should include the decrease of  $k_1$  with evolution (Jiang et al. 2010), or the decrease of  $\frac{k_2}{k_1}$  due to the differential rotation of the components (Hilditch 2001). The latter has been proposed as a mechanism for the energy transfer between the components (Yakut & Eggleton 2005; Eggleton 2010b).

Looking at the prototype of mergers, V1309 Sco, that was dominated in its final stage by  $L_2$  mass loss, another possible explanation is that the non-conservative mass and angular momentum loss drives the Darwin criterion and the instability mass ratio to lower values, as proposed by Pejcha et al. (2017). Nevertheless, since the progenitor of V1309 Sco is proposed to be an eclipsing contact binary with period of about 1.4 d (Tylenda et al. 2011), maybe larger period systems need to be observed in contact phase. These are few and represent the very end of contact binaries with periods 1.3–1.5 d in the period distribution as initially noticed by Rucinski (1998) and is still confirmed in the plethora of new discoveries of surveys (Li et al. 2019; Jayasinghe et al. 2020). However, in the model proposed by Stępień (2011) the primary of the pre-burst contact binary V1309 Sco is a giant that recently filled its Roche lobe and whose contact phase is very short. Thus, the proposed progenitors of mergers may differ from EWs in both evolutionary state and duration of the contact phase. Considering the rapid period decay of V1309 Sco preceding the merging, we suggest to search for systems with large orbital period change rates ( $dP/dt$ ) in photometric surveys, in combination with detailed study of their evolutionary state through high-accuracy spectroscopic observations (Rucinski 2020), reconsidering the energy transfer models between the components and including systematic monitoring of times of minima of the already proposed merger candidates.

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## DATA AVAILABILITY

The data underlying this paper are available in the paper and in its online supplementary material.

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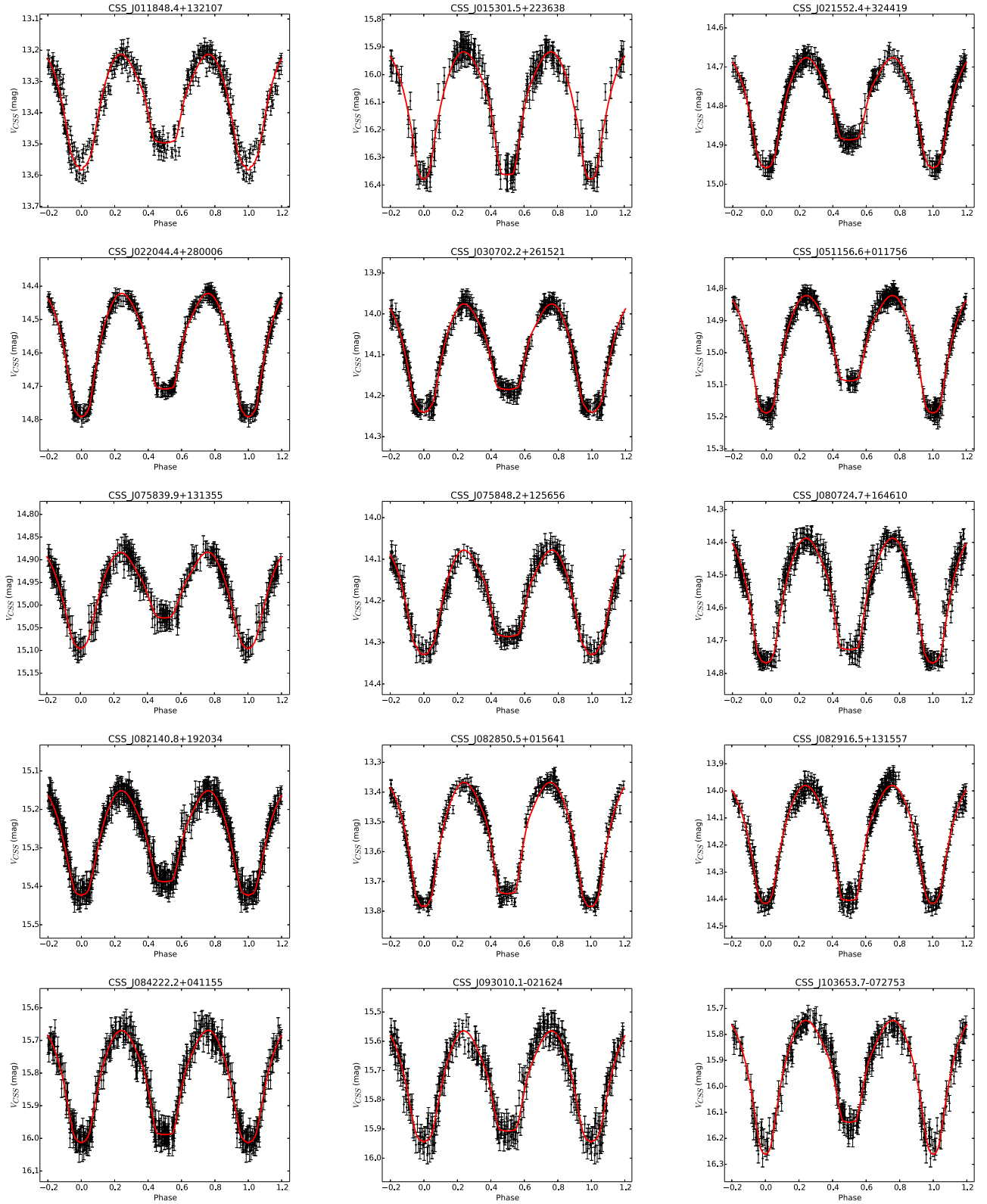


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## APPENDIX A: PREVIOUS LMRS AND 30 NEW CSS LMRS

In this appendix, we provide 1) the observed LCs and the best fitted models of the 30 new CSS LMR systems (Figure A1) and 2) a compilation of LMRS, along with their parameters, from the literature and derived in this work (Table A1). The columns are organized as follows (from left to right): name, where (n) represents LMRS not included in Latković et al. (2021) and \* represents LMRS with LCs used for sample 2; period (in d); mass ratio ( $q$ ); method used to determine the mass ratio: photometric with total eclipses (T) or spectroscopic (SP); primary mass ( $M_1$ ); primary radius ( $R_1$ ); secondary radius ( $R_2$ ); fill-out factor ( $f$ ); the derived ratio of total spin angular to orbital momentum  $\frac{J_s}{J_o}$  for gyration radii  $k^2 = 0.06$  (this work); the derived ratio of total spin angular to orbital momentum  $\left(\frac{J_s}{J_o}\right)_k$  for different values of  $k_1^2$  for the massive component and  $k_2^2 \sim 0.205$  for the less massive component (this work); and references.



**Figure A1.** The observed LCs (black points) and the best-fitting models (red line) for the 30 new CSS LMR systems.



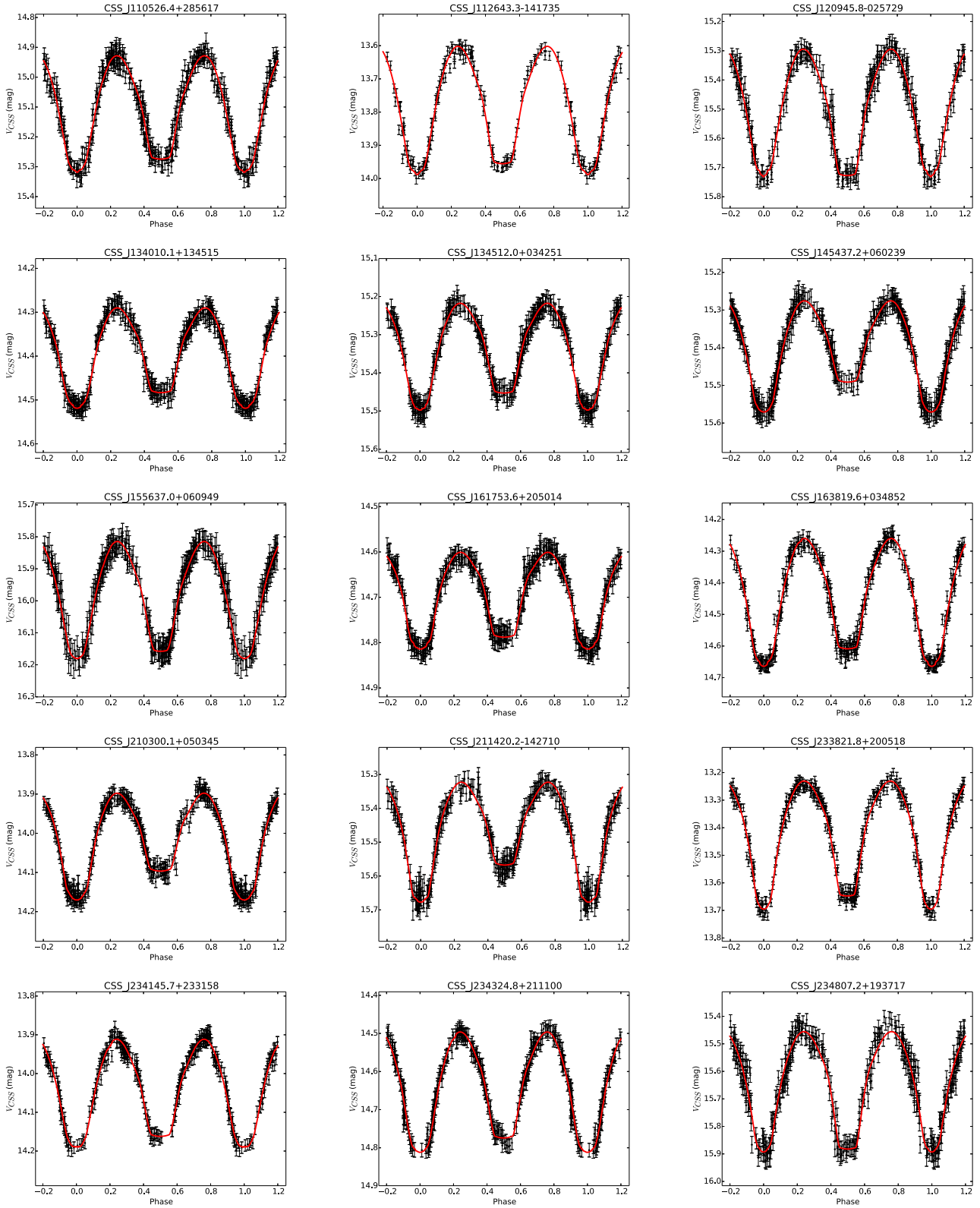


Figure A1. *continued.*

Table A1. Parameters of previously known LMRs.

| Name                    | Period<br>(d) | $q$           | Type | $M_1$<br>( $M_\odot$ ) | $R_1$<br>( $R_\odot$ ) | $R_2$<br>( $R_\odot$ ) | $f$           | $\frac{J_c}{J_0}$ | $\left(\frac{J_c}{J_0}\right)_k$ | Reference                                  |
|-------------------------|---------------|---------------|------|------------------------|------------------------|------------------------|---------------|-------------------|----------------------------------|--|
| V1187 Her               | 0.31076       | 0.044         | T    |                        |                        |                        | 0.801         | 0.612             |                                  | Caton et al. (2019)                        |
| KIC 4244929*            | 0.34140       | 0.059         | T    | 1.481                  | 1.521                  | 0.477                  | 0.809         | 0.439             | 0.227                            | Şenavcı et al. (2016)                      |
| KIC 9151972*            | 0.38680       | 0.059         | T    | 1.606                  | 1.696                  | 0.528                  | 0.760         | 0.438             | 0.231                            | Şenavcı et al. (2016)                      |
| KIC 11097678*           | 0.99972       | 0.064 (0.097) | T    | 2.960                  | 3.897                  | 1.264                  | 0.801 (0.87)  | 0.401             | 0.259                            | Şenavcı et al. (2016); Zola et al. (2017)  |
| ASAS J083241+2332.4*    | 0.31132       | 0.065         | T    | 1.220                  | 1.34                   | 0.42                   | 0.506         | 0.398             | 0.354                            | Sriram et al. (2016)                       |
| V857 Her*               | 0.38223       | 0.065         | T    |                        |                        |                        | 0.837         | 0.395             |                                  | Qian et al. (2005b)                        |
| KIC 8539720*            | 0.74450       | 0.067 (0.158) | T    | 2.438                  | 2.955                  | 0.929                  | 0.473 (0.860) | 0.372             | 0.223                            | Şenavcı et al. (2016); Zola et al. (2017)  |
| KIC 3127873*            | 0.67153       | 0.073 (0.109) | T    | 2.268                  | 2.69                   | 0.899                  | 0.65 (0.88)   | 0.342             | 0.201                            | Şenavcı et al. (2016); Zola et al. (2017)  |
| KIC 12352712*           | 0.72207       | 0.073         | T    | 2.377                  | 2.859                  | 0.944                  | 0.566         | 0.339             | 0.203                            | Şenavcı et al. (2016)                      |
| AW UMa                  | 0.43872       | 0.076 (0.099) | SP   |                        |                        |                        | 0.487         | 0.323             |                                  | Eaton (2016); Rucinski (2015)              |
| ZZ PsA                  | 0.37388       | 0.078         | T    | 1.213                  | 1.422                  | 0.559                  | 0.970         | 0.298             | 0.284                            | Wadhwa et al. (2021b)                      |
| M4 V53                  | 0.30845       | 0.078         | T    | 1.472                  | 1.383                  | 0.481                  | 0.690         | 0.320             | 0.168                            | Li et al. (2017)                           |
| SX Crv                  | 0.31660       | 0.079         | SP   | 1.246                  | 1.347                  | 0.409                  | 0.272         | 0.303             | 0.283                            | Zola et al. (2004)                         |
| KIC 10007533*           | 0.64806       | 0.081 (0.101) | T    | 2.199                  | 2.566                  | 0.881                  | 0.535 (0.178) | 0.301             | 0.177                            | Şenavcı et al. (2016); Zola et al. (2017)  |
| V870 Ara*               | 0.39972       | 0.082         | SP   | 1.503                  | 1.61                   | 0.61                   | 0.984         | 0.310             | 0.166                            | Szalai et al. (2007)                       |
| KIC 8145477*            | 0.56578       | 0.082 (0.102) | T    | 2.012                  | 2.26                   | 0.767                  | 0.40 (0.650)  | 0.244             | 0.167                            | Şenavcı et al. (2016); Zola et al. (2017)  |
| KIC 11144556*           | 0.64298       | 0.087 (0.161) | T    | 2.174                  | 2.542                  | 0.927                  | 0.730 (0.97)  | 0.281             | 0.166                            | Şenavcı et al. (2016); Zola et al. (2017)  |
| KIC 10596883*           | 0.46891       | 0.088         | T    | 1.772                  | 1.882                  | 0.641                  | 0.182         | 0.266             | 0.147                            | Şenavcı et al. (2016)                      |
| KIC 8804824*            | 0.45740       | 0.091 (0.111) | T    | 1.738                  | 1.829                  | 0.628                  | 0.137 (0.67)  | 0.255             | 0.140                            | Şenavcı et al. (2016); Zola et al. (2017)  |
| KR Com (n)              | 0.40797       | 0.093         | SP   | 0.880                  | 1.445                  | 0.505                  | 0.990         | 0.286             | 0.489                            | Gazeas et al. (2021a)                      |
| KIC 7698650*            | 0.59916       | 0.095 (0.123) | T    | 2.064                  | 2.357                  | 0.876                  | 0.605 (0.700) | 0.253             | 0.148                            | Şenavcı et al. (2016); Zola et al. (2017)  |
| FP Boo                  | 0.64048       | 0.096         | SP   | 1.614                  | 2.31                   | 0.774                  | 0.394         | 0.245             | 0.140                            | Gazeas et al. (2006)                       |
| KIC 9453192*            | 0.71884       | 0.099 (0.155) | T    | 2.314                  | 2.734                  | 1.01                   | 0.438 (0.620) | 0.238             | 0.145                            | Şenavcı et al. (2016); Zola et al. (2017)  |
| XX Sex                  | 0.54011       | 0.1           | SP   | 1.301                  | 1.87                   | 0.696                  | 0.476         | 0.236             | 0.177                            | Deb & Singh (2011)                         |
| UCAC4 479–113711        | 0.35292       | 0.1           | T    | 1.400                  | 1.47                   | 0.58                   | 0.893         | 0.204             | 0.119                            | El-Sadek et al. (2019)                     |
| NW Aps                  | 1.06556       | 0.1           | T    |                        |                        |                        | 0.446         | 0.237             |                                  | Wadhwa (2005)                              |
| AW CrB*                 | 0.36094       | 0.101         | T    |                        |                        |                        | 0.750         | 0.244             |                                  | Broens (2013)                              |
| KIC 9350889*            | 0.72595       | 0.102 (0.106) | T    | 2.322                  | 2.775                  | 1.068                  | 0.631 (0.870) | 0.234             | 0.144                            | Şenavcı et al. (2016); Zola et al. (2017)  |
| ASAS J165139+2255.7*    | 0.35321       | 0.103         | T    | 1.030                  | 1.27                   | 0.46                   | 0.600         | 0.216             | 0.291                            | Alton (2018)                               |
| DN Boo                  | 0.44757       | 0.103         | SP   | 1.428                  | 1.71                   | 0.67                   | 0.644         | 0.234             | 0.127                            | Şenavcı et al. (2008)                      |
| FG Hya                  | 0.32783       | 0.104         | SP   | 1.445                  | 1.438                  | 0.515                  | 0.698         | 0.244             | 0.134                            | Zola et al. (2010)                         |
| KIC 10229723*           | 0.62872       | 0.105 (0.145) | T    | 2.110                  | 2.363                  | 0.852                  | 0.023 (0.35)  | 0.213             | 0.126                            | Şenavcı et al. (2016); Zola et al. (2017)  |
| ASAS J082243+1927.0     | 0.28000       | 0.106         | T    | 1.100                  | 1.15                   | 0.42                   | 0.719         | 0.225             | 0.266                            | Kandulapati, Devarapalli & Pasagada (2015) |
| GR Vir                  | 0.34697       | 0.106         | SP   | 1.376                  | 1.49                   | 0.55                   | 0.932         | 0.232             | 0.167                            | Gazeas et al. (2005)                       |
| V1191 Cyg*              | 0.31339       | 0.107         | SP   | 1.283                  | 1.292                  | 0.503                  | 0.577         | 0.221             | 0.184                            | Ostadezhad, Delband & Hasanazadeh (2014)   |
| ASAS J025115–2525.4     | 0.55927       | 0.107         | T    | 1.680                  | 2.07                   | 0.579                  | 0.092         | 0.203             | 0.115                            | Saygan (2016)                              |
| KIC 7601767*            | 0.48673       | 0.107         | T    | 1.784                  | 1.925                  | 0.74                   | 0.449         | 0.219             | 0.125                            | Şenavcı et al. (2016)                      |
| CK Boo                  | 0.35515       | 0.111         | SP   | 1.584                  | 1.533                  | 0.65                   | 0.946         | 0.221             | 0.125                            | Deb & Singh (2011)                         |
| TYC 6995–813-1 (n)      | 0.38318       | 0.111         | T    | 1.230                  | 1.46                   | 0.6                    | 0.720         | 0.243             | 0.223                            | Wadhwa et al. (2021a)                      |
| V1222 Tau*              | 0.29173       | 0.112         | T    | 0.900                  | 1.06                   | 0.42                   | 0.532         | 0.209             | 0.349                            | Liu et al. (2015)                          |
| NSVS 3198272            | 0.35228       | 0.115         | T    | 1.621                  | 1.479                  | 0.583                  | 0.391         | 0.198             | 0.111                            | Kjurkchieva et al. (2019b)                 |
| KIC 6118779*            | 0.36425       | 0.117         | T    | 1.465                  | 1.512                  | 0.657                  | 0.922         | 0.209             | 0.118                            | Şenavcı et al. (2016)                      |
| V2787 Ori               | 0.81098       | 0.12          | T    | 1.440                  | 2.45                   | 0.96                   | 0.181         | 0.186             | 0.102                            | Tian, Zhu & Wang (2019)                    |
| AL Lep                  | 0.44864       | 0.12          | T    |                        |                        |                        | 0.627         | 0.199             |                                  | Wadhwa (2005)                              |
| KIC 10395609*           | 0.36425       | 0.121         | T    | 1.460                  | 1.504                  | 0.657                  | 0.916         | 0.167             | 0.093                            | Şenavcı et al. (2016)                      |
| Cl* NGC 6121 SAW V66    | 0.26997       | 0.123         | T    | 1.660                  | 1.24                   | 0.5                    | 0.322         | 0.184             | 0.105                            | Liu, Qian & Fernández-Lajús (2011)         |
| KIC 10618253*           | 0.43740       | 0.125         | SP   | 1.476                  | 1.703                  | 0.756                  | 0.930         | 0.195             | 0.111                            | Şenavcı et al. (2016)                      |
| $\epsilon$ CrA          | 0.59143       | 0.128         | SP   | 1.700                  | 2.1                    | 0.85                   | 0.268         | 0.175             | 0.101                            | Yang et al. (2005a)                        |
| KIC 12055014            | 0.49991       | 0.128 (0.16)  | T    | 1.781                  | 1.939                  | 0.819                  | 0.597 (0.670) | 0.182             | 0.107                            | Şenavcı et al. (2016); Zola et al. (2017)  |
| V776 Cas                | 0.44042       | 0.13          | SP   | 1.550                  | 1.71                   | 0.73                   | 0.646         | 0.180             | 0.103                            | Zhou et al. (2016b)                        |
| ASAS J102556+2049.3     | 0.28498       | 0.131         | T    | 0.710                  | 1.06                   | 0.39                   | 0.240         | 0.207             | 0.456                            | Kjurkchieva et al. (2019b)                 |
| V902 Sgr                | 0.29394       | 0.132         | T    | 1.400                  | 1.234                  | 0.513                  | 0.389         | 0.172             | 0.096                            | Samec & Corbin (2002)                      |
| ASAS J050334–2521.9     | 0.41406       | 0.133         | T    | 1.260                  | 1.54                   | 0.6                    | 0.535         | 0.171             | 0.146                            | Gezer & Bozkurt (2016)                     |
| KIC 8265951*            | 0.77996       | 0.134 (0.154) | T    | 2.364                  | 2.816                  | 1.175                  | 0.365 (0.380) | 0.143             | 0.107                            | Şenavcı et al. (2016); Zola et al. (2017)  |
| ASAS J040633–4729.4     | 0.40637       | 0.136         | T    | 1.330                  | 1.54                   | 0.6                    | 0.324         | 0.164             | 0.127                            | Saygan (2016)                              |
| DZ Psc*                 | 0.36613       | 0.136         | SP   | 1.370                  | 1.46                   | 0.67                   | 0.987         | 0.179             | 0.129                            | Yang et al. (2013)                         |
| HV Aqr                  | 0.37450       | 0.14          | SP   | 1.240                  | 1.456                  | 0.601                  | 0.740         | 0.175             | 0.163                            | Gazeas et al. (2021a)                      |
| HV Aqr                  | 0.37446       | 0.145         | SP   | 1.355                  | 1.448                  | 0.648                  | 0.568         | 0.159             | 0.118                            | Li & Qian (2013a)                          |
| ASAS J142124+1813.1 (n) | 0.24300       | 0.14          | T    | 2.730                  | 1.43                   | 0.57                   | 0.230         | 0.177             | 0.118                            | Kjurkchieva et al. (2019b)                 |
| V677 Cen                | 0.32500       | 0.142         | T    |                        |                        |                        | 0.341         | 0.158             |                                  | Barone et al. (1993)                       |
| V710 Mon                | 0.40520       | 0.143         | T    | 1.140                  | 1.46                   | 0.66                   | 0.627         | 0.166             | 0.189                            | Liu et al. (2014b)                         |
| V410 Aur*               | 0.36636       | 0.144         | SP   | 1.270                  | 1.37                   | 0.59                   | 0.290         | 0.154             | 0.136                            | Luo et al. (2017)                          |
| HN UMa                  | 0.38260       | 0.145         | SP   | 1.279                  | 1.42                   | 0.61                   | 0.285         | 0.153             | 0.132                            | Oh et al. (2007)                           |
| KIC 9776718 (n)         | 0.5444        | 0.146         | T    | 4.880                  | 2.9                    | 1.32                   | 0.915         | 0.165             | 0.139                            | Li et al. (2020)                           |
| GSC 1042–2191           | 0.42380       | 0.146         | T    | 1.260                  | 1.54                   | 0.69                   | 0.650         | 0.161             | 0.146                            | Bulut, Bulut & Demircan (2016)             |
| NSVS 1917038            | 0.31807       | 0.146         | T    |                        |                        |                        | 0.037         | 0.147             |                                  | Guo et al. (2020)                          |
| KIC 2159783*            | 0.37388       | 0.147         | T    | 1.451                  | 1.496                  | 0.694                  | 0.800         | 0.162             | 0.095                            | Şenavcı et al. (2016)                      |
| XY LMi*                 | 0.43689       | 0.148         | T    |                        |                        |                        | 0.741         | 0.159             |                                  | Qian et al. (2011)                         |
| EM Psc                  | 0.34396       | 0.149         | T    |                        |                        |                        | 0.953         | 0.163             |                                  | Qian et al. (2008)                         |
| ASAS J113031–0101.9 (n) | 0.27100       | 0.15          | T    |                        |                        |                        | 0.500         | 0.153             |                                  | Pribulla, Vanko & Hambalek (2009)          |
| TYC 4157–0683-1         | 0.39607       | 0.15          | T    | 1.367                  | 1.499                  | 0.667                  | 0.763         | 0.157             | 0.115                            | Acerbi, Barani & Martignoni (2014)         |
| Mis V1395               | 0.73930       | 0.15          | T    |                        |                        |                        | 0.869         | 0.160             |                                  | Guo et al. (2020)                          |
| V1179 Her (n)           | 0.38551       | 0.153         | T    | 1.300                  |                        |                        | 0.450         | 0.151             | 0.112                            | Broens (2021)                              |
| V1511 Her (n)           | 0.35008       | 0.154         | T    |                        |                        |                        | 0.480         |                   |                                  | Broens (2021)                              |
| ASAS J063546+1928.6     | 0.47553       | 0.154         | T    | 1.230                  | 1.184                  | 0.19                   | 0.571         | 0.149             | 0.144                            | Sriram et al. (2018)                       |
| AH Cnc                  | 0.36046       | 0.156         | T    | 1.188                  | 1.332                  | 0.592                  | 0.510         | 0.144             | 0.151                            | Peng et al. (2016)                         |
| NGC 6397 V8             | 0.27124       | 0.159         | T    | 0.876                  | 0.995                  | 0.456                  | 0.461         | 0.141             | 0.248                            | Li & Qian (2013c)                          |
| KIC 3104113*            | 0.84679       | 0.159 (0.167) | T    | 2.440                  | 3.085                  | 1.538                  | 0.947 (0.910) | 0.152             | 0.105                            | Şenavcı et al. (2016); Zola et al. (2017)  |
| Cl* NGC 6715 SAW V144   | 0.72159       | 0.16          | T    | 1.310                  | 2.23                   | 0.95                   | 0.195         | 0.135             | 0.111                            | Li & Qian (2013b)                          |
| NSVS 1926064            | 0.40747       | 0.16          | T    | 1.558                  | 1.605                  | 0.755                  | 0.708         | 0.146             | 0.089                            | Kjurkchieva, Popov & Petrov (2020b)        |

Table A1 – continued

| Name                           | Period<br>(d) | $q$           | Type | $M_1$<br>( $M_\odot$ ) | $R_1$<br>( $R_\odot$ ) | $R_2$<br>( $R_\odot$ ) | $f$           | $\frac{J_s}{J_0}$ | $\left(\frac{J_s}{J_0}\right)_k$ | Reference   |
|--------------------------------|---------------|---------------|------|------------------------|------------------------|------------------------|---------------|-------------------|----------------------------------|---|
| EF Dra                         | 0.42403       | 0.16          | SP   | 1.815                  | 1.702                  | 0.777                  | 0.467         | 0.140             | 0.087                            | Yang (2012)                                       |
| V902 Cep                       | 0.32870       | 0.162         | T    | 1.077                  | 1.208                  | 0.563                  | 0.470         | 0.139             | 0.178                            | Kjurkchieva et al. (2019b)                        |
| NSVS 2256852                   | 0.34888       | 0.162         | T    | 0.950                  | 1.18                   | 0.52                   | 0.170         | 0.134             | 0.210                            | Kjurkchieva et al. (2019b)                        |
| V1695 Aql                      | 0.41283       | 0.162         | T    |                        |                        |                        | 0.831         | 0.147             |                                  | Samec et al. (2017)                               |
| V972 Her                       | 0.44309       | 0.164         | SP   | 0.910                  | 1.35                   | 0.59                   | 0.01          | 0.129             | 0.215                            | Selam et al. (2018)                               |
| V1115 Cas                      | 0.32329       | 0.164         | T    | 1.049                  | 1.181                  | 0.548                  | 0.424         | 0.137             | 0.184                            | Kjurkchieva et al. (2019b)                        |
| GSC 03517–00663                | 0.29502       | 0.164         | T    |                        |                        |                        | 0.692         | 0.142             |                                  | Guo et al. (2015)                                 |
| Cl* NGC 104 WSB V95            | 0.27890       | 0.165         | T    | 0.970                  | 1.05                   | 0.49                   | 0.743         | 0.138             | 0.212                            | Liu, Qian & Fernández Lajús (2014a)               |
| AH Aur                         | 0.49411       | 0.165         | SP   | 1.674                  | 1.897                  | 0.837                  | 0.750         | 0.149             | 0.092                            | Gazeas et al. (2005)                              |
| TV Mus                         | 0.44568       | 0.166         | SP   | 1.350                  | 1.7                    | 0.83                   | 0.742         | 0.141             | 0.110                            | Qian et al. (2005a)                               |
| V445 Cep                       | 0.44878       | 0.167         | SP   |                        |                        |                        | 0.517         | 0.123             |                                  | Oh, Kim & Sung (2010)                             |
| EPIC 211957146*                | 0.35502       | 0.17          | T    | 1.050                  | 1.1                    | 0.23                   | 0.642         | 0.136             | 0.183                            | Sriram et al. (2017)                              |
| V345 Gem                       | 0.27477       | 0.171         | SP   | 1.371                  | 1.134                  | 0.486                  | 0.11          | 0.128             | 0.092                            | Gazeas et al. (2021a)                             |
| NSVS 13602901 (n)              | 0.52389       | 0.171         | T    | 1.190                  | 1.69                   | 0.79                   | 0.440         | 0.131             | 0.138                            | Wadhwa et al. (2021a)                             |
| V1542 Aql                      | 0.41754       | 0.171         | T    |                        |                        |                        | 0.555         | 0.113             |                                  | Wadhwa (2004)                                     |
| TYC 1337–1137-1 (n)*           | 0.47550       | 0.172         | T    | 1.386                  | 1.7                    | 0.83                   | 0.760         | 0.138             | 0.100                            | Liao et al. (2017)                                |
| AS CrB*                        | 0.38066       | 0.172         | T    | 1.250                  | 1.4                    | 0.67                   | 0.592         | 0.133             | 0.126                            | Liu et al. (2017)                                 |
| II UMa                         | 0.82522       | 0.172         | SP   | 1.990                  | 2.8                    | 2.41                   | 0.869         | 0.139             | 0.092                            | Zhou et al. (2016a)                               |
| OU Ser                         | 0.29677       | 0.173         | SP   | 1.187                  | 1.155                  | 0.544                  | 0.667         | 0.129             | 0.137                            | Deb & Singh (2011)                                |
| ASAS J002821–1453.3            | 0.40266       | 0.173         | T    | 1.330                  | 1.49                   | 0.6                    | 0.397         | 0.132             | 0.102                            | Gezer & Bozkurt (2016)                            |
| KIC 5439790*                   | 0.79609       | 0.174 (0.192) | T    | 2.314                  | 2.764                  | 1.29                   | 0.296 (0.360) | 0.126             | 0.085                            | Şenavcı et al. (2016); Zola et al. (2017)         |
| KIC 8496820*                   | 0.43697       | 0.176         | T    | 1.566                  | 1.655                  | 0.803                  | 0.596         | 0.130             | 0.081                            | Şenavcı et al. (2016)                             |
| PZ UMa                         | 0.26267       | 0.178         | T    | 0.770                  | 0.92                   | 0.43                   | 0.396         | 0.124             | 0.257                            | Zhou & Soonthornthum (2019)                       |
| V728 Her                       | 0.47129       | 0.178         | SP   | 1.800                  | 1.87                   | 0.82                   | 0.810         | 0.111             | 0.072                            | Erkan & Ulaş (2016)                               |
| CSS J075258.0+382035           | 0.42991       | 0.178         | T    | 1.040                  | 1.44                   | 0.7                    | 0.628         | 0.130             | 0.070                            | Kjurkchieva et al. (2019b)                        |
| GSC 3599–2569                  | 0.40291       | 0.18          | T    |                        |                        |                        | 0.247         | 0.119             |                                  | Gorda, Lyaptev & Sobolev (2015)                   |
| TYC 3700–1384 (n)              | 0.40747       | 0.182         | T    | 1.450                  |                        |                        | 0.490         |                   |                                  | Broens (2021)                                     |
| GSC 4778–152                   | 0.51746       | 0.182         | T    |                        |                        |                        | 0.304         | 0.119             |                                  | Tuvikene et al. (2008)                            |
| TY Pup (n)                     | 0.81920       | 0.184         | T    | 1.650                  | 2.636                  | 1.373                  | 0.843         | 0.129             | 0.084                            | Sarotsakulchai et al. (2018)                      |
| CN Hyi                         | 0.45611       | 0.184         | SP   | 1.370                  | 1.6                    | 0.77                   | 0.420         | 0.120             | 0.074                            | Özkardeş, Erdem & Bakış (2009)                    |
| V2388 Oph (n)                  | 0.80230       | 0.186         | SP   | 1.800                  | 2.6                    | 1.3                    | 0.650         | 0.123             | 0.081                            | Yakut, Kalomeni & İbanoğlu (2004)                 |
| GV Leo                         | 0.26673       | 0.188         | T    |                        |                        |                        | 0.178         | 0.113             |                                  | Kriwattanawong & Poojion (2013)                   |
| TYC 3836–0854-1 (n)            | 0.41557       | 0.19          | T    | 1.200                  | 1.46                   | 0.75                   | 0.794         | 0.125             | 0.134                            | Liao et al. (2017)                                |
| BO Ari*                        | 0.31819       | 0.19          | SP   | 0.995                  | 1.09                   | 0.515                  | 0.494         | 0.118             | 0.176                            | Gürol, Gürsoytrak & Bradstreet (2015)             |
|                                | 0.31819       | 0.207         | SP   | 1.095                  | 1.19                   | 0.636                  | 0.757         | 0.113             | 0.147                            | Porro et al. (2021)                               |
| V619 Peg                       | 0.38872       | 0.19          | T    | 2.020                  | 1.642                  | 0.811                  | 0.521         | 0.118             | 0.079                            | Kjurkchieva et al. (2019b)                        |
| HV UMa                         | 0.35539       | 0.19          | SP   | 2.800                  | 2.62                   | 1.18                   | 0.770         | 0.107             | 0.077                            | Csák et al. (2000)                                |
| V1853 Ori                      | 0.38300       | 0.19          | T    | 1.200                  | 1.36                   | 0.66                   | 0.333         | 0.114             | 0.121                            | He et al. (2019)                                  |
| IK Per                         | 0.67603       | 0.191         | T    | 1.990                  | 2.4                    | 1.15                   | 0.521         | 0.118             | 0.079                            | Zhu et al. (2005)                                 |
| Y Sex                          | 0.48774       | 0.195         | SP   | 1.471                  | 1.568                  | 0.795                  | 0.596         | 0.117             | 0.075                            | Deb & Singh (2011)                                |
| VW Vul                         | 0.38451       | 0.195         | T    |                        |                        |                        | 0.403         | 0.112             |                                  | Capezzali, Fiorucci & Spogli (2008)               |
| EX Leo                         | 0.40860       | 0.2           | SP   | 1.573                  | 1.56                   | 0.734                  | 0.366         | 0.112             | 0.071                            | Zola et al. (2010)                                |
| V402 Aur                       | 0.60350       | 0.2           | SP   | 1.638                  | 1.997                  | 0.915                  | 0.031         | 0.103             | 0.066                            | Zola et al. (2004)                                |
| KIC 5809868                    | 0.43939       | 0.201         | T    |                        |                        |                        | 0.470         | 0.112             |                                  | Zola et al. (2017)                                |
| NSVS 9045055                   | 0.35459       | 0.202         | T    | 1.990                  | 1.51                   | 0.751                  | 0.302         | 0.108             | 0.073                            | Kjurkchieva et al. (2019b)                        |
| EL Aqr                         | 0.48141       | 0.203         | SP   | 1.570                  | 1.73                   | 0.87                   | 0.440         | 0.109             | 0.071                            | Wadhwa & Zealey (2004)                            |
| NSVS 7328383                   | 0.27208       | 0.205         | T    | 1.013                  | 1                      | 0.49                   | 0.171         | 0.104             | 0.151                            | Kjurkchieva, Popov & Petrov (2019a)               |
| DN Aur                         | 0.61689       | 0.205         | T    |                        |                        |                        | 0.468         | 0.108             |                                  | Goderya, Leung & Schmidt (1996)                   |
| UY UMa                         | 0.37602       | 0.206         | T    | 1.151                  | 1.342                  | 0.696                  | 0.606         | 0.112             | 0.131                            | Kim et al. (2019)                                 |
| HI Pup                         | 0.43257       | 0.206         | SP   | 1.210                  | 1.44                   | 0.67                   | 0.203         | 0.103             | 0.108                            | Ulaş & Ulusoy (2014)                              |
| TYC 3836–0854-1*               | 0.41556       | 0.206         | T    | 1.383                  | 1.5                    | 0.763                  | 0.592         | 0.110             | 0.085                            | Acerbi et al. (2014)                              |
| ASAS J212236+0657.3            | 0.29395       | 0.207         | T    | 0.807                  | 0.793                  | 0.665                  | 0.132         | 0.102             | 0.200                            | Kjurkchieva et al. (2020a)                        |
| TZ Boo*                        | 0.29716       | 0.207         | SP   | 0.990                  | 1.08                   | 0.56                   | 0.531         | 0.108             | 0.165                            | Christopoulou, Parageorgiou & Chrysopoulos (2011) |
| TYC 2402–0643-1 (n)            | 0.39943       | 0.208         | T    | 0.860                  | 1.22                   | 0.67                   | 0.220         | 0.103             | 0.188                            | Samec, Caton & Faulkner (2020)                    |
| NSVS 6859986                   | 0.38357       | 0.208         | T    | 1.870                  | 1.63                   | 0.84                   | 0.860         | 0.115             | 0.078                            | Kjurkchieva et al. (2019b)                        |
| GSC 03950–00707 (n)            | 0.41200       | 0.21          | T    | 2.850                  | 1.85                   | 0.91                   | 0.120         | 0.100             | 0.076                            | Kjurkchieva et al. (2019b)                        |
| GM Dra                         | 0.33875       | 0.21          | SP   | 1.213                  | 1.252                  | 0.606                  | 0.230         | 0.105             | 0.110                            | Gazeas et al. (2005)                              |
| CV Cyg                         | 0.98343       | 0.21          | T    | 1.600                  |                        |                        | 0.490         | 0.108             | 0.072                            | Vinko, Hegedus & Hendry (1996)                    |
| RR Cen                         | 0.60569       | 0.21          | SP   | 1.820                  | 2.1                    | 1.05                   | 0.351         | 0.104             | 0.070                            | Yang et al. (2005a)                               |
| MM Com (n)                     | 0.30199       | 0.215         | T    | 0.790                  | 0.99                   | 0.35                   | 0.240         | 0.095             | 0.184                            | Kjurkchieva et al. (2019b)                        |
| V409 Hya                       | 0.47227       | 0.216         | T    | 1.500                  | 1.69                   | 0.9                    | 0.606         | 0.106             | 0.071                            | Na et al. (2014)                                  |
| V816 Cep                       | 0.31141       | 0.219         | T    | 2.830                  | 1.576                  | 0.836                  | 0.511         | 0.103             | 0.080                            | Kjurkchieva et al. (2019b)                        |
| MW Pav*                        | 0.79499       | 0.22          | SP   | 1.514                  | 2.412                  | 1.277                  | 0.693         | 0.105             | 0.070                            | Alvarez et al. (2015)                             |
| V604 Car                       | 0.47229       | 0.22          | T    |                        |                        |                        | 0.380         | 0.101             |                                  | Wadhwa (2006)                                     |
| PY Boo                         | 0.27805       | 0.222         | T    | 0.790                  | 0.93                   | 0.47                   | 0.180         | 0.096             | 0.195                            | Kjurkchieva et al. (2019b)                        |
| FN Cam                         | 0.67713       | 0.222         | SP   | 2.400                  | 2.61                   | 1.44                   | 0.880         | 0.110             | 0.084                            | Pribulla et al. (2002)                            |
| NSVS 7051868                   | 0.51760       | 0.223         | T    | 1.610                  | 1.8                    | 0.94                   | 0.353         | 0.097             | 0.066                            | Barani, Martignoni & Acerbi (2017)                |
| AQ Psc                         | 0.47561       | 0.226         | SP   | 1.661                  | 1.708                  | 0.891                  | 0.350         | 0.095             | 0.065                            | Deb & Singh (2011)                                |
| V921 Her                       | 0.87738       | 0.226         | SP   | 1.784                  | 2.56                   | 1.29                   | 0.190         | 0.090             | 0.061                            | Zhou et al. (2016c)                               |
| V921 Her                       | 0.87738       | 0.244         | SP   | 2.068                  | 2.752                  | 1.407                  | 0.230         | 0.088             | 0.061                            | Gazeas et al. (2006)                              |
| KIC 9832227                    | 0.45796       | 0.228         | SP   | 1.395                  | 1.581                  | 0.83                   | 0.430         | 0.096             | 0.074                            | Molnar et al. (2017)                              |
| 1SWASP J000437.82+033301.2 (n) | 0.26150       | 0.23          | T    | 0.820                  | 0.89                   | 0.46                   | 0.116         | 0.091             | 0.177                            | Latković & Čeki (2021)                            |
| V2357 Oph                      | 0.41557       | 0.231         | SP   | 1.160                  | 1.386                  | 0.705                  | 0.322         | 0.093             | 0.109                            | Deb & Singh (2011)                                |
| ASAS J035020–8017.4            | 0.62240       | 0.232         | T    | 0.990                  | 1.76                   | 0.87                   | 0.344         | 0.094             | 0.144                            | Saygan (2016)                                     |
| YY CrB                         | 0.37656       | 0.232         | SP   | 1.393                  | 1.385                  | 0.692                  | 0.228         | 0.091             | 0.070                            | Gazeas et al. (2005)                              |
| YY CrB                         | 0.37656       | 0.243         | SP   | 1.430                  | 1.43                   | 0.81                   | 0.634         | 0.104             | 0.098                            | Vaňko et al. (2004)                               |
| TYC 5532–1333-1                | 0.47449       | 0.232         | T    | 1.510                  | 1.67                   | 0.9                    | 0.343         | 0.095             | 0.065                            | Devarapalli et al. (2020)                         |
| GSC 0763–0572                  | 0.42640       | 0.233         | T    | 1.230                  | 1.434                  | 0.757                  | 0.310         | 0.092             | 0.097                            | Wang et al. (2012)                                |



Table A1 – continued

| Name             | Period<br>(d) | $q$   | Type | $M_1$<br>( $M_\odot$ ) | $R_1$<br>( $R_\odot$ ) | $R_2$<br>( $R_\odot$ ) | $f$   | $\frac{J_k}{J_0}$ | $\left(\frac{J_k}{J_0}\right)_k$ | Reference                           |
|------------------|---------------|-------|------|------------------------|------------------------|------------------------|-------|-------------------|----------------------------------|-------------------------------------|
| DU Boo           | 1.05589       | 0.234 | SP   | 2.080                  | 3.19                   | 1.74                   | 0.502 | 0.082             | 0.060                            | Djurašević et al. (2013)            |
| V1094 Cas        | 0.51400       | 0.235 | T    |                        |                        |                        | 0.300 | 0.093             |                                  | Wadhwa (2019)                       |
| V789 Her         | 0.32004       | 0.236 | T    | 1.130                  | 1.15                   | 0.62                   | 0.238 | 0.091             | 0.114                            | Li et al. (2018)                    |
| V2741 Cyg        | 0.31600       | 0.236 | T    |                        |                        |                        | 0.480 | 0.096             |                                  | Wadhwa (2019)                       |
| NSVS 4803568 (n) | 0.28657       | 0.238 | T    | 0.790                  | 0.93                   | 0.43                   | 0.090 | 0.086             | 0.172                            | Kjurkchieva et al. (2019b)          |
| FO Hya           | 0.46956       | 0.238 | T    | 1.310                  | 1.62                   | 0.91                   | 0.689 | 0.098             | 0.091                            | Prasad et al. (2013)                |
| GSC 3208–1986    | 0.40466       | 0.24  | T    |                        |                        |                        | 0.390 | 0.092             |                                  | Samec et al. (2015)                 |
| KIC 10267044     | 0.43004       | 0.24  | T    |                        |                        |                        | 0.550 | 0.097             |                                  | Zola et al. (2017)                  |
| V507 Lyr         | 0.36691       | 0.24  | T    |                        |                        |                        | 0.200 | 0.089             |                                  | Wetterer et al. (2004)              |
| HR Boo*          | 0.31597       | 0.241 | T    | 1.210                  | 1.17                   | 0.62                   | 0.180 | 0.090             | 0.098                            | Kjurkchieva et al. (2019b)          |
| V404 Peg         | 0.41918       | 0.243 | SP   | 1.175                  | 1.346                  | 0.71                   | 0.321 | 0.089             | 0.103                            | Gürol et al. (2011)                 |
| GSC 0804–0118    | 0.32369       | 0.243 | T    |                        |                        |                        | 0.200 | 0.087             |                                  | Yang et al. (2005b)                 |
| KIC 3221207      | 0.47383       | 0.244 | T    | 1.300                  | 1.67                   | 0.87                   | 0.790 | 0.096             | 0.090                            | Aliçavuş & Soyduğan (2017)          |
| T-Dra0-00959 (n) | 0.32933       | 0.245 | T    | 0.890                  | 1.06                   | 0.5                    | 0.240 | 0.084             | 0.147                            | Kjurkchieva et al. (2019b)          |
| UW CVn           | 0.29247       | 0.245 | T    |                        |                        |                        | 0.202 | 0.086             |                                  | Kopacki & Pigulski (1995)           |
| TYC 01963–0488-1 | 0.42704       | 0.248 | T    | 1.370                  | 1.46                   | 0.78                   | 0.347 | 0.088             | 0.073                            | Alton (2016)                        |
| HI Dra           | 0.59742       | 0.25  | SP   | 0.720                  | 1.98                   | 1.08                   | 0.240 | 0.085             | 0.061                            | Papageorgiou & Christopoulou (2015) |
| KN Per           | 0.86650       | 0.25  | T    |                        |                        |                        | 0.545 | 0.090             |                                  | Yang & Qian (2015)                  |

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