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Impact of Ensemble-Variational Data Assimilation in Heavy Rain Forecast over Brazilian Northeast

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Abstract: The Brazilian Northeast (BNE) is located in the tropical region of Brazil. It is bounded by the Atlantic Ocean, and its climate and vegetation are strongly affected by continental plateaus. The plateaus keep the humid air masses to the east and are responsible for the rain episodes, and at the west side the northeastern hinterland and dry air masses are observed. This work is a case study that aims to evaluate the impact of updating the model initial condition using the 3DEnVar (Three-Dimensional Ensemble Variational) system in heavy rain episodes associated with Mesoscale Convective Systems (MCS). The results were compared to 3DVar (Three-Dimensional Variational) and EnSRF (Ensemble Square Root Filter) systems and with no data assimilation. The study enclosed two MCS cases occurring on 14 and 24 January 2017. For that purpose, the RMS (Regional Modeling System) version 3.0.0, maintained by the Center for Weather Forecasting and Climate Studies (CPTEC), used two components: the Weather Research and Forecasting (WRF) mesoscale model and the GSI (Gridpoint Statistical Interpolation) data assimilation system. Currently, the RMS provides the WRF initial conditions by using 3DVar data assimilation methodology. The 3DVar uses a climatological covariance matrix to minimize model errors. In this work, the 3DEnVar updates the RMS climatological covariance matrix through the forecast members based on the errors of the day. This work evaluated the improvements in the detection and estimation of 24 h accumulated precipitation in MCS events. The statistic index RMSE (Root Mean Square Error) showed that the hybrid data assimilation system (3DEnVar) performed better in reproducing the precipitation in the MCS occurred on 14 January 2017. On 24 January 2017, the EnSRF was the best system for improving the WRF forecast. In general, the BIAS showed that the WRF initialized with different initial conditions overestimated the 24 h accumulated precipitation. Therefore, the viability of using a hybrid system may depend on the hybrid algorithm that can modify the weights attributed to the EnSRF and 3DVar matrix in the GSI over the assimilation cycles.

Keywords: 3DEnVar; mesoscale convective systems; WRF; GSI

1. Introduction

Accurate weather forecasts of severe weather phenomena that affects the economy across the globe are essential for short to long-term planning of various human activities in order to avoid socio-economic damage caused by natural disasters (e.g., landslides and floods). For the Brazilian Northeast (BNE), which is the region of study of this work, according to data from the portal of the National Confederation of Cities [1] for a long dry period, BNE had losses totaled in the order of BRL 52 billion between 2012 and 2015. For the same region, intense rain events have caused deaths, floods, and rupture of dams, causing many social and economic losses in only one day [2].

It is essential to have a good representation of the initial conditions of the atmosphere in order to obtain an accurate weather forecast. The initialization of Numerical Weather Predictions (NWP) means calculating many dynamic and thermodynamic parameters. An



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Copyright: © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). alternative method for improving the initial conditions for an NWP model is by using Data Assimilation (DA). DA systems organize the information in the model's grid using the best estimation of the initial state. Thus, DA techniques must combine observations (e.g., meteorological, oceanographic, or hydrological) with a background. The result is the best initial condition for the NWP models initialization [3].

Initially, a subjective DA method used the same wind velocity values (isopleths) to interpolate the observation fields. The scheme was known as Subjective Interpolation [4]. This scheme demanded an experienced synoptic meteorologist and many days of work (e.g., data preparation and remotion of observational errors), which resulted in hard work for operational application.

An important fact to consider is that meteorological observations are not perfect because of intrinsic observation errors and human interference (e.g., parallax errors). In order to avoid observation errors, a climatology, the mean of neighbor stations, and a weather forecast may be the reference in the DA algorithm schemes [5]. If large differences between observed and background data exist, the observation should not be considered in the DA procedure.

Many objective analysis schemes were developed during the last century. These schemes replaced subjective interpolation by avoiding manual errors caused by erroneous meteorologist's interpretations. From that perspective, References [4,6] introduced a polynomial interpolation method, and [7] developed a Successive Correction Method (SCM). A similar SCM method, introduced by [8] gained notoriety. This method combines meteorological observational data with the model background in order to improve initial conditions. Afterwards, a statistical correction method acquired notoriety when it was compared with SCM, and it was presented to the scientific community by [9,10]. Finally, the Variational Method (VM) was introduced by [11], and a spectral operational DA system by [12].

In general, DA divides into sequential and non-sequential techniques [13]. Sequential methods (e.g., 3DVar and EnSRF) consist of the DA methods where many analysis cycles are applied at each time step in order to obtain a new model initial condition. Non-sequential methods (e.g., 4DVar) corrects the model trajectory when the observations are available in a typical forecast time window of 6 h.

The Center for Weather Forecasting and Climate Studies at the National Institute for Space Research (CPTEC/INPE in Portuguese) developed the Regional Modelling System (RMS), which allow coupling different weather forecast models such as WRF and DA systems such as GSI (Gridpoint Statistical Interpolation) and WRFDA (WRF DA system). RMS permits updating the initial condition from the CPTEC's operational WRF model with conventional and non-conventional datasets using the GSI system, and it allows performing 3DVar, EnSRF, and 3DEnVar DA.

Encouraging results have been obtained in several studies using 3DEnVar DA. Reference [14] observed that the hybrid using the radar radial speed produces better analysis and prediction compared to the result without DA during Hurricane Ika (2008). Reference [15] used hybrid DA with radar data to improve the analysis and predictions of a storm event on 20 May 1977, near Dell City in Oklahoma and obtained satisfactory results. Reference [16] carried out a detailed study using the CPTEC global model in order to assess the ability of the hybrid system to assimilate data from conventional stations, satellites, and predict certain variables. The conclusion was that the 3DEnVar had better results compared to 3DVar in all cases. The benefits obtained by using the 3DEnVar were due to the errors of the day incorporated into the background covariance matrix.

Therefore, the main objective of this work is to incorporate daily forecast errors to update analyses by EnSRF using the 3DEnVar and to evaluate how the hybrid DA system (3dEnVar) can improve the daily precipitation forecast by the WRF model during Mesoscale Convective Systems (MCS) events occurred over the Brazilian Northeast (BNE).

2. Materials and Methods

The MCS events studied in this work occurred on 14th and 24th January 2017. These two cases were selected because they were the two most heavy-rain events in 2017 over Maranhao state. Both cases were associated with Mesoscale Convective Systems (MCS) and generated 24 h accumulated precipitation over 70 mm. According to [17], the BNE has high occurrence of MCS. This work presents an impact evaluation of the 3DVar and 3DEnVar DA systems in improving precipitation forecasts from the WRF model for a domain over the BNE. Thereby, Section 2 illustrates the 3DVar and 3DEnVar main characteristics, the WRF configurations, and a description of the statistic metrics used to evaluate the DA analyses and WRF forecasts.

2.1. Location of the Study Area

BNE (Figure 1) is located in the tropical portion of Brazil between the equator (0° S) and Capricorn parallels (23.5° S). The mean surface temperature of this region is around 20 degrees Celsius, and it has a heterogeneous topography (at the coast it has plains bounded by the Atlantic Ocean, and at the hinterland it has highlands responsible for the dry meteorological conditions).



Figure 1. Brazilian Northeast topographic domain (m).

The domain showed in Figure 1 was also used to assess the rainfall events associated with MCS over the BNE using the WRF model and satellite rainfall estimates. The domain area chosen in this study considered the dynamic and geographic particularities of the synoptic systems (e.g., upper-level cyclonic vortex, Intertropical Convergence Zone, and sea breeze) that produce MCS in BNE.

2.2. Convective Systems Identification

MCS is a cloud system with an area of equal to or more than 3500 km^2 , and the cloud top brightness temperature is equal to or less than -38.5 degrees Celsius [18]. The infrared

channel images from the GOES-13 (Geostationary Operational Environmental Satellite-13) sensor provided the cloud top brightness temperature, and they are available at the Division of Meteorological Satellites and Sensors website (http://satelite.cptec.inpe.br/, (accessed on 25 August 2021)).

2.3. Rain Events Identification

The 24 h accumulated precipitation observations were obtained from the National Meteorological Institute (INMET). It was useful for identifying heavy rain precipitation episodes that occurred over BNE meteorological stations. The heavy rain precipitation, in this work, is an event in which the 24 h accumulated precipitation registered by the BNE meteorological stations was greater than 70 mm occurring on 14 and 24 January 2017. This reference value is the same one adopted by the National Center for Monitoring and Early Warning of Natural Disasters (CEMADEN), available on https://www.gov.br/mcti/pt-br/rede-mcti/cemaden, (accessed on 25 August 2021).

In order to spatially evaluate the WRF heavy rain forecasts over the BNE, the MERGE data [19] were chosen. The MERGE is an operational product produced and distributed by CPTEC. It combines the observed precipitation with the estimate of precipitation by satellite. Therefore, the MERGE algorithm combines the Integrated Multi-satellite Retrievals for GPM (IMERG) and TRMM Multisatellite Precipitation Analysis (TRMM-TMPA) with observations, and the final data are available with 0.1 degrees horizontal resolution.

2.4. WRF Mesoscale Model

WRF is a NWP model developed by the National Center for Atmospheric Research (NCAR), from the University Corporation for Atmospheric Research (UCAR). It is the most widely used dynamical downscaling numerical weather forecasting and research model. The WRF model is also continuously improved and supported by a wide international atmospheric science research community [20].

This work used Advanced Research WRF 3.9.1.1, the same operational version used by CPTEC. The WRF consists of two dynamic cores, a DA system and a software architecture structure, which supports parallel computing applied to solve a series of meteorological problems ranging from the meter scale to thousands of kilometers [21].

The WRF model used the same parameterizations defined by [22], except for the Cumulus cloud parameterizations. This modification occurred because the climatological study [23] for the tropical region between 2012 and 2016 summer showed that the new Tiedke schemes combined with RRTMG were the best schemes for reproducing diurnal precipitation cycle between 45 degrees north–south. The authors in [23] compared the new Tiedke [24], the Tiedke [25], the Kain–Fritsch [26], and the new simplified Arakawa–Schubert schemes [27]. Moreover, the parameterizations used in our study (Table 1) are the same ones employed by CPTEC in its operational WRF model.

Table 1. The WRF model configurations.

Parameters	Configurations
Model	WRF
Horizontal Resolution	9 km
Global Model	GEFS [28]
Topographic data	SRTM (30 m) [29]
Soil data	MODIS (925 m)
Radiation model	RRTMG [30]
Vertical levels	42 sigma-pressure
Microphysics	WSM6 [31]
Cumulus	New Tiedtke [24]
Planetary boundary	YSU [32]
Surface model	Noah [33]

The GEFS [28] is an ensemble NWP model from the National Centers for Environmental Prediction (NCEP), consisting of 21 members with a horizontal and vertical resolution of 1 degree and 64 vertical levels. Although GEFS forecasts are currently available four times a day on a 0.5 degrees latitude-longitude grid, we used the 0000 UTC initialized runs on a 1.0 degree latitude-longitude grid since this is the only initialization time and output grid spacing available on the NCEP NOMADS server for the MCS forecast periods.

The WRF initial conditions were from GEFS, and GEFS was updated by 3DVar, EnSRF, and 3DEnVar DA systems. The 3DVar system updated only the GEFS control member, and the EnSRF and 3DEnVar updated the 21 forecast members from GEFS (20 perturbations + 1 control member). For later times in the 6 h cycle, the WRF 6 h forecasts were updated by 3DVar, EnSRF, and 3DEnVar. Therefore, a 6 h cycle from 12 and 22 to 14 (MCS 1) and 24 January (MCS 2) 0000 UTC was performed, and 72/48/24 h forecasts were initiated at 12/13/14 January 0000 UTC (MCS 1) and 22/23/240000 UTC (MCS 2). The precipitation forecasts identified by f72, f48, and f24 stands for the 24 h accumulated precipitation forecasts valid for 14 January (MCS 1) and 24 (MCS 2) and initiated at each 0000 UTC cycle as mentioned above.

2.5. The Gridpoint Statistical Interpolation

The Regional Modelling System from CPTEC used in this work applied the Gridpoint Statistical Interpolation (GSI) DA scheme to update the analyses. Thus, in order to update the forecasts, GEFS (in the first assimilation cycle) and WRF data (in the other assimilation cycles) were combined with meteorological observations using 3DEnVar DA systems.

2.5.1. Data Assimilated

At the analysis step in the assimilation cycle, the GSI used the radiance data from the Advanced Microwave Sounding Unit-A (AMSU-A); the data from the Meteorological Operational Satellite Program (METOP)-A/B and Microwave Humidity Sounder (MHS) containing microwave moisture sounding information from NOAA-18, 19, and METOP-A/B satellites data; the High-Resolution Infrared Radiation Sounder 4 (HIRS4) data, with radiance from NOAA-18, 19, and METOP-A/B satellites; observational wind data by satellite, curvature angle data, and GPS radio-concealment, plus data from conventional and automatic weather stations on the surface; and radiosonde, for zonal and southern winds, temperature, specific humidity, and surface pressure, available at the following website: https://rda.ucar.edu, (accessed on 25 August 2021).

2.5.2. 3DVar Variational Method

The 3DVar uses an iterative method to generate atmospheric analyses based on an algorithm that requires an efficient solution search process (e.g., the conjugate gradient minimization algorithm).

The main objective of the variational problem is to find a minimum variance analysis that minimizes the cost function (Equation (1)). In order to perform this, it is necessary to calculate the difference between the state estimate **x** and the background \mathbf{x}_b weighted by the inverse error of the background error covarianvce **B** in addition to the difference between the observation vector \mathbf{y}_0 and the background state at the physical space $\mathbf{H}(\mathbf{x})$, weighted by the inverse of the observation error covariance matrix **R**.

$$J(\mathbf{x}) = \frac{1}{2} (\mathbf{x} - \mathbf{x}_{\mathbf{b}})^T \mathbf{B}^{-1} (\mathbf{x} - \mathbf{x}_{\mathbf{b}}) + \frac{1}{2} [\mathbf{y}_{\mathbf{o}} - H(\mathbf{x})]^T (\mathbf{R})^{-1} [\mathbf{y}_{\mathbf{o}} - H(\mathbf{x})]$$
(1)

In Equation (1), the vector $\mathbf{x} - \mathbf{x}_{\mathbf{b}}$ represents the analysis increment (errors). In the same expression, $\mathbf{y} - H(\mathbf{x})$ is the innovation, with *H* being the non-linear observation operator responsible for bringing the state vector to be analyzed to the physical space of the observation.

The NMC method [34] was used in this work to generate the climatological background error statistics (**B**). A dataset containing 3 months of cold-start 24 h forecasts over the entire South America covering the Southern Hemisphere during the summer was produced every day starting at 0000 and 1200 UTC. The differences between the 24 and 12 h forecasts valid at the same time were used to calculate the domain-averaged background error statistics.

In order to obtain the analysis equation, it is necessary to calculate the gradient of J(1) and to equal it to zero ($\nabla J(\mathbf{x}) = 0$). Considering that the state vector to be analyzed is equal to the analysis vector $\mathbf{x} = \mathbf{x}_{\mathbf{a}}$ and that this is very close to the real state of the atmosphere, it is possible to obtain Equation (2) with values around the observations and from the background.

$$\mathbf{x}_{\mathbf{a}} = \mathbf{x}_{\mathbf{b}} + (\mathbf{B}^{-1} + \mathbf{H}^{T}\mathbf{R}^{-1}\mathbf{H})^{-1}[(\mathbf{H}^{T}\mathbf{R}^{-1})(\mathbf{y}_{\mathbf{o}} - \mathbf{H}(\mathbf{x}_{\mathbf{b}}))]$$
(2)

2.5.3. The Ensemble Square-Root Filter

The Ensemble Square Root Filter (EnSRF), used in the RMS, updates the analysis variables within the domain over the BNE already pre-processed by the WRF. References [35,36] show that this methodology has superior numerical accuracy and stability compared to the standard Kalman filter algorithm and avoids sampling problems associated with the use of perturbed observations.

The GSI EnSRF [37] uses the equations of the ensemble mean member (3), and it updates the analysis in the ensemble perturbation space (5) to obtain the initial conditions. In order to perform this, the GSI uses the Equations (3)–(6). Unlike the terms already presented in previous subtopics, the overbars denote the ensemble mean in Equation (3) for the analysis terms and the background. The single quotes, overwritten in Equation (5), represent the perturbations (ensemble of analysis that represent different situations of the atmosphere for the same given time and place).

$$\overline{\mathbf{x}_{\mathbf{a}}} = \overline{\mathbf{x}_{\mathbf{b}}} + \mathbf{K}[\mathbf{y}_{\mathbf{o}} - H(\overline{\mathbf{x}_{\mathbf{b}}})]$$
(3)

$$\tilde{\mathbf{K}} = \alpha \mathbf{K} \tag{4}$$

$$\mathbf{x}'_{\mathbf{a}} = \mathbf{x}'_{\mathbf{b}} + \tilde{\mathbf{K}}H(\mathbf{x}'_{\mathbf{b}}) \tag{5}$$

$$\alpha = \left[1 + \sqrt{\frac{R}{\mathbf{H}\mathbf{P}^{b}\mathbf{H}^{T} + R}}\right]^{-1}$$
(6)

Note that in Equation (4), the matrix $\tilde{\mathbf{K}}$ is the gain matrix that is essential for generating analysis for the ensemble perturbed members at a time after assimilation (\mathbf{x}'_{a}) and obtained through Equation (5). In the EnSRF analyses, the observations are not perturbed; therefore, they are determined through the perturbed members at a time before the analysis generation (e.g., GEFS ensemble) plus the gain obtained by applying the matrix $\tilde{\mathbf{K}}$ to the GEFS ensemble members. The ensemble mean analysis ($\overline{\mathbf{x}}_{a}$) is the result of the average of ensemble predictions and the analysis increments weighted by the Kalman gain matrix (\mathbf{K}). Equations (3) and (5) together compose a set of analysis responsible for updating the background by the EnSRF algorithm.

The Kalman gain matrix (**K**) in Equations (3) and (4) represent a relation between the the multivariate background error covariance matrix (**B**), and the observation covariance matrix (**R**) is defined as Equation (7).

$$\mathbf{K} = \mathbf{P}^{\mathbf{b}} \mathbf{H}^{T} [\mathbf{H} \mathbf{P}^{\mathbf{b}} \mathbf{H}^{T} + \mathbf{R}]^{-1}$$
(7)

The term $\mathbf{P}^{\mathbf{b}}$ from Equation (7) denotes the covariance matrix of the forecast errors, which for the EnSRF is calculated by means of the background state perturbations $\mathbf{x}_{n}^{'\mathbf{b}}$,

which in turn are calculated as the difference between each ensemble member (n) and the ensemble mean. **P**^b is given in Equation (8), as shown in [37].

$$\mathbf{P}^{\mathbf{b}} = \frac{1}{(n-1)} \sum_{i=1}^{n} \mathbf{x}_{\mathbf{n}}^{'\mathbf{b}} (\mathbf{x}_{\mathbf{n}}^{'\mathbf{b}})^{T}$$
(8)

2.5.4. Three-Dimensional Ensemble-Variational

In the 3DEnVar, the model error covariance matrix (**B**) is a linear combination of the static matrix of 3DVar (\mathbf{B}_{3DVar}) and the one updated by the EnSRF ($\mathbf{P}^{\mathbf{b}}$), as shown in Equation (9). At the end of the analysis step, the 3DEnVar cost function is minimized by using the hybrid background error covariance matrix using the linear combination of the matrices, as shown in Equation (9).

$$\mathbf{B} = (1 - \alpha)\mathbf{B}_{3DVar} + \alpha \mathbf{P}^{\mathbf{b}}$$
⁽⁹⁾

In Equation (9), α is the coefficient used to weigh the contribution of the two matrices. This work used the optimal weights of 0.75 for EnSRF and 0.25 for 3DVar.

The RMS version used in this work tested the settings for a hybrid assimilation system with weights for the ensemble background error covariance of 50, 75, and 100%, trying to reproduce the same experiment of very short-term weather forecasts Rapid Refresh, RAP [38]. Based on the single observation test, the best analyses results were with an ensemble background error covariance of 75%, similar to the results of [38]. With the weight of 75%, the analyses increment have fields influencing more grid points in the horizontal and vertical, contributing to the matrix taking its contribution to more grid points away from the observation location.

2.6. Statistical Data Analysis

The contingency table indexes (Equations (10)–(14)) plotted in a performance diagram were used to show the WRF 24 h accumulated precipitation forecast performance by using initial conditions updated by 3DVar, EnSRF, and 3DEnVar. They evaluated the WRF performance for all experiments over the Maranhão state surface meteorological stations (Figure 2), which is the region where MCS occurred.

In order to quantify the Probability of Detection (POD), False Alarms (FAR), errors, and hits, the contingency table [39] was calculated and described by Equations (10) and (11), respectively. The FAR and POD range from 0 to 1. The FAR index has better performances when its value is closer to 0, while the POD indicated better performances when its value was closer to 1.

$$FAR = \frac{\text{false alarm}}{\text{false alarm} + \text{hits}}$$
(10)

$$POD = \frac{\text{hits}}{\text{hits} + \text{errors}}$$
(11)

Another method for evaluating the performance of a given estimate is to calculate the Success Rate (SR) obtained by the ratio of the number of hits by the total number of hits plus false alarms, as shown in Equation (12). Thus, for values close to one, the estimate is accurate.

$$TS = \frac{\text{hits}}{\text{hits} + \text{false alarm}}$$
(12)

The frequency BIAS (Equation (13)) shows the relationship between the number of estimated events and the number of observed events. The calculation results will return values greater than zero. Values closer to one indicate better performances, and values greater than or less than one indicate that the occurrence of events was, respectively, overestimated and underestimated.

$$BIAS = \frac{\text{false alarm + hits}}{\text{hits + errors}}$$
(13)

The Critical Success Index (CSI) was calculated (Equation (14)) for the accumulated rainfall estimates obtained from different data sources. By using the CSI, it is possible to observe the percentage of correct answers, deducting the number of times that the non-occurrence of events correctly predicted the events. Values close to one indicate good performances.

$$CSI = \frac{\text{hits}}{\text{false alarm + hits + errors}}$$
(14)

The Root Mean Square Error (RMSE), Equation (15)) also showed how the 24 h accumulated precipitation from the WRF model is distant from the observational data and the accuracy of the model data. In order to conduct this, it was necessary to use the surface meteorological stations over Maranhão as the references.

$$RMSE = \sqrt{\left(\frac{1}{N}\sum_{i=1}^{N} (\mathbf{x_i} - \mathbf{y_o})^2\right)}$$
(15)



Figure 2. The map represents the topography (m) and the INMET meteorological stations over Maranhão state (red circles).

3. Results and Discussion

3.1. Convective Rainfall

The intense rain episodes on the BNE, evaluated in this study, occurred on 14th and 24th January 2017 in the cities of Barra da Corda (5.51° S and 45.24° W) and Colinas (6.03° S and 44.23° W), respectively. Both cities are in the most continental portion of the state of Maranhão, as illustrated in Figure 2.

The MCS1 (the event that took place on 14 January 2017) covered a total surface area of 218,000 km², during the maximum development stage, with cloud top temperatures below -80 °C. This system caused heavy rain events mainly over the central region of Maranhão, around 6° S and 46° W, where rainfall accumulated in 24 h recorded by the conventional INMET station in Barra da Corda (MA) was equivalent to 72.5 mm (Figure 3).



Figure 3. MERGE 24 h accumulated precipitation over the BNE (mm) for the MCS1 event.

Referring to Figure 3, it is possible to observe an area with intense daily rain episodes over the state of Maranhão greater than 50 mm. This region was under the influence of a convective systems, and it caused the heavy rain (greater than 70 mm) reported by the INMET surface meteorological station in the Barra da Corda region (6° S and 46° W).

For 24 January 2017, the daily accumulated rainfall field obtained from MERGE (Figure 4) is illustrated over the city of Colinas (6° S and 44° W), with precipitation above 50 mm for the area of influence of the MCS.

The MCS2 (the event that took place on 24 January 2017) covered a total surface area of 143,000 km² during the maximum development stage, with cloud top temperatures below -80 °C. This system caused heavy rain events recorded by INMET surface stations (equal to 72 mm) over the central-east region of Maranhão.

Thus, for the two days with records of heavy rains over the cities in the Maranhão state, MERGE estimates indicated a large volume of rain (around 75 mm), proving to be a particularly effective product in the characterization of precipitation accumulated in 24 h during episodes of MCS over BNE that occurred on 14th and 24th January 2017.



Figure 4. MERGE 24 h accumulated precipitation over the BNE (mm) for the MCS2 event.

3.2. Total of Assimilated Data

In general, the number of observations used during the DA procedure for pressure, specific humidity, temperature, and wind speed was similar to those presented in Figure 5 along with DA cycles. The assimilated data in both MCS are similar and both present large amounts of wind data due to the availability of Atmospheric Motion Vectors (AMV) data, obtained from satellite observations.

Unfortunatelly, the limited availability of conventional meteorological data in the northeast region of Brazil may affect the performance of the DA, which can result in a lower skill of the WRF forecasts.

3.3. WRF 24-h Accumulated Precipitation

The predictions performed by the WRF model regarding 24 h accumulated rainfall for 14th January 2017 (Figure 6) reveal that, in general, all the experiments were able to produce rainfall events superior to 5 mm over the region of Barra da Corda (6° S and 45° W), in Maranhão. The WRF forecasts have spatial distributions similar to the 24 h accumulated rain fields obtained from the MERGE (Figure 3).

Despite the similarity between the MERGE 24 h rainfall fields, the predictions of the f24h experiment (Figure 6), in general, present a large area covering the state of Maranhão, with daily rainfall accumulations superior to 5 mm, when using the initial conditions of GEFS, EnSRF, and 3DEnVar, respectively, to the f24h-WRF, f24h-EnSRF, and f24h-3DEnVar experiments (Figure 6). Otherwise, the precipitation data from the WRF model initialized with the 3DVar analysis (experiment f24-3DVar, in Figure 6) presented a drier atmosphere (with fewer precipitation areas greater than 5 mm covering the state of Maranhão compared with the others experiments) for f24h-WRF, f24h-EnSRF, and f24h-3DEnVar (Figure 6). As a



result, f24h-3DVar (Figure 6) had an inferior performance when compared with the others experiments.



Figure 7 shows the RMSE of 24, 48, and 72 h forecast among the experiments evaluated on 14th January 2017. The f24h-3DVar had the worst performance compared to f24h-WRF, f24h-EnSRF, and f24h-3DEnVar. Thus, the model errors compared with INMET observations on the state of Maranhão were around 22 mm for the f24h experiments (WRF, EnSRF, and 3DEnVar), and the model error was greater than 25 mm in the f24h-3DVar. Among the many reasons for the f24h-3DVar's lower performance was the 3DVar static covariance matrix of forecast errors in time. Therefore, the model errors represented by this matrix may not represent the errors of the fields represented in the background for the whole year or in the MCS presence in the tropical region, which can result in rainfall forecasts that differ from the observations. The justification is because the numerical weather prediction models are sensitive to initial conditions, and any errors in initial conditions make a few of weather predictions performed by the WRF model equations reliable.



Figure 6. The 24 (f24h), 48 (f48h), and 72 h (f72h) hours forecast relative to WRF 24 h rain precipitation over the BNE (mm) for the SMC1 event, without initial conditions updated by GSI (WRF), and the initial conditions updated by the EnSRF, 3DVar, and 3DEnVar GSI algorithm.



Figure 7. The 24 (f24h), 48 (f48h), and 72 (f72h) hours forecast relative to the WRF RMSE of forecasted 24 h accumulated precipitation over the BNE (mm) for the SMC1 event, without initial conditions updated by GSI (WRF), and the initial conditions updated by the EnSRF, 3DVar, and 3DEnVar GSI algorithm.

The best 24 h WRF precipitation performance accumulated rainfall field was for the experiments Figure 7-f24h-3DEnVar and f24h-EnSRF. Note in Figure 7, that the forecast errors obtained in these configurations are around 22 mm, the smallest among the experiments. The good RMSE performances illustrated in Figure 7-f24h-3DEnVar and f24h-EnSRF occurred because the analysis in EnSRF and 3DEnVar uses the background error covariance matrix to update the initial conditions with the error of the day. Thus, this matrix updates at each assimilation cycle with the error of the day calculated from ensemble forecast members, as shown in Equation (8). The ensemble methodology contributes to obtaining initial conditions that minimize the systematic errors of the background used in DA and contributes to rainfall forecasts closer to those observed in meteorological stations.

The best WRF model predictions for f48h and f72h experiments (Figure 6) used 3DEn-Var analyses, for which its forecast errors regarding INMET meteorological observations on the state of Maranhão were around 23 mm for both experiments. Otherwise, the WRF forecast model initialized with the 21 EnSRF analyses (for the f48h and f72h experiments) obtained the worse RMSE values from the experiment, with errors superior to 25 mm in both experiments (Figure 7). This performance of the WRF model initialized with the EnSRF analyses suggested that ensemble predictions used to obtain the EnSRF background error covariance matrix were very small. Thus, the limited ensemble member numbers represent a small ensemble of atmospheric conditions, which resulted in an EnSRF matrix with a low potential for representing the atmospheric model errors in the experiment and an increase in forecast errors.

In summary, among the evaluated experiments, the one that presented the best performance in the 24 h rainfall accumulated forecast for 14 January 2017 was the WRF model started with the 3DEnVar analyses. Therefore, on 14 January 2017, the hybrid matrix of 3DEnVar contributed to minimizing the rain forecast errors.

The WRF model predictions for 24 January 2017 (Figure 8) illustrate that, for all experiments, it was possible to predict rainfall events with a threshold greater than 5 mm over the Colinas region (6° S and 44° W) where the MCS episode took place. Furthermore, a simple comparison shows a similar spatial distribution of the MERGE 24 h accumulated rainfall field, and it is represented by the different predictions of the WRF model depicted in Figure 8. However, in general, the predicted values underestimated the daily rainfall obtained by MERGE.



Figure 8. RMSE of 24 h accumulated precipitation (mm) started at 24 (f24h), 48 (f48h), and 72 h (f72h) before SMC2 event day over the BNE (mm), without initial conditions updated by GSI (WRF), and the initial conditions updated by EnSRF, 3DVar, and 3DEnVar GSI algorithm.

The MERGE 24 h accumulated rainfall fields show a similar distribution of precipitation over the BNE, as illustrated in Figure 8. The RMSE showing a notorious difference between analysis and the INMET meteorological observations on the Maranhão state is in the Figure 8-f24h-WRF experiment. For this experiment, the errors can be as great as 35 mm.

The best WRF forecast performance started 24 h before the SCM2 was the experiment f24h-EnSRF (Figure 9). The experiment f48h-EnSRF also had small forecast errors when compared with INMET meteorological stations. Thus, in the Figure 9-f24h-EnSRF and f48h-EnSRF experiments, a set of predictions initialized with analysis from the EnSRF that obtained a small prediction error of f24h and f48h experiments is portrayed, as shown by the RMSE value around 28 mm.





The worst performance of the f48h experiment was obtained by the WRF model initialized with the 3DVar analysis, with an error of 35 mm referring to the RMSE (Figure 9). As discussed previously in this section, the 3DVar static background error covariance matrix may be one of the source of this lower skill. The static matrix may not represent accuracy systems such MCS2, and the introduction of the errors of the day by the ENSRF or 3DEnVar improves the representations of this system.

In the f72h experiment, initialized with the 3DVar, EnSRF, and 3DEnVar analyses, the errors were superior (around 33 mm) to the WRF model errors initialized with the GEFS analysis, with values referring to the RMSE around 28 mm (Figure 9). This situation may be due to the fact that the analysis fields generated in the RMS through 3DVar, EnSRF, and 3DEnVar were not able to minimize the background errors when updating the analyses.

The Figure 9-f72h-WRF experiment used the GEFS control member as an initial condition. As this control member is from a DA system used by the NCEP for the generation of analysis (the EnSRF), the results obtained in the f72h-WRF experiment performed well. This is in part attributed to the initial conditions obtained from the EnSRF, which were able to reduce background errors and consequently helped the WRF model in obtaining better performance in rainfall forecast compared to the other experiments evaluated in Figure 8.

In summary, for the predictions of the WRF model valid for 24th January 2017, the importance of DA by set in the best performance of the WRF model initialized with GEFS and EnSRF is noted. The lower WRF model performance initialized with the 3DVar and 3DEnVar analyses suggests a deficiency of the static background error covariance matrix in correcting the forecast errors. This deficiency could be diminished by assigning a higher weight to the EnSRF covariance matrix in 3DEnVar and/or by obtaining a new static matrix.

3.4. WRF Rainfall Forecast by Performance Diagram

The performance diagram for the 24 h accumulated precipitation from the WRF model initialized 24 h in advance (MCS1 and MCS2) illustrates that the probability of detection (POD) for events with a higher threshold of 5 mm forecasted by the WRF model initialized with 3DEnVar analysis was the highest value among the evaluated experiments Figure 10 (POD equivalent to 100%). Likewise, by the diagram shown in Figure 10, the success rate of the WRF experiments initialized with 3DEnVar analysis performed satisfactorily, reaching a success rate equivalent to 80%, the highest among the evaluated experiments. This fact demonstrates that the predictions of the WRF experiment having the 3DEnVar analysis



as an initial condition performed well in terms of the rainfall accumulated in 24 h for a threshold greater than 5 mm.

Figure 10. Performance diagram for the WRF model daily rainfall initialized with GEFS and the initial conditions of EnSRF, 3DVar, and 3DEnVar for the 14th and 24th January 2017, initialized 24 h earlier.

The frequency BIAS of the performance diagram, Figures 10 and 11, illustrates that WRF experiments generated by one of the evaluated DA systems, in general, overestimated the meteorological observations, as well as the predictions of the WRF model initialized with the GEFS control member.

Similarly to the daily accumulated rainfall performed by the WRF model that was started 24 h earlier with the initial conditions of 3DEnVar, the forecasts started 48 h earlier with the same settings and managed to return a high POD for the rain events equivalent to 100%. It was the best result among the evaluated experiments (Figure 11). The analysis updated by 3DEnVar also had a good performance associated with the success rate (greater than 60%). This finding revealed that this configuration also performed well in detecting the absence of rain when the INMET surface stations did not register rain.

The forecast of accumulated rainfall in 24 h of the WRF model started 72 h earlier with 3DEnVar analysis (Figure 12) showed a POD greater than 70% for the days of intense rain occurrence over the Maranhão state. Despite this fact, they did not have the best performance among the evaluated configurations regarding POD, which for the other experiments (WRF, 3DVar, and EnSRF) were superior to 80%. The success rate for the predictions updated by the 3DEnVar initial conditions performed the same as verified in the previous experiments. The success rate values were superior to 60% when the predicted values, as illustrated by the frequency BIAS (Figure 12), overestimated the observations and underestimated the accumulated rainfall observed on 14th and 24th January 2017, respectively.



Figure 11. Performance diagram for the WRF model daily rainfall initialized with GEFS and the initial conditions of EnSRF, 3DVar, and 3DEnVar, for 14 and 24 January 2017, initialized 48 h earlier.



Figure 12. Performance diagram for the WRF model daily rainfall initialized with GEFS and the initial conditions of EnSRF, 3DVar, and 3DEnVar, for 14 and 24 January 2017, initialized 72 h earlier.

The best performances obtained in the 24 h accumulated rain forecast were from the WRF model initialized with the 3DEnVar analysis on the points of the meteorological station of INMET, on the state of Maranhão, as depicted by calculating the contingency table indices and reference [16]. Thus, the best performance of the WRF model for the 24 and 48 h forecasts using the initial conditions updated by 3DEnVar occurred due to the combination of the analysis updated by 3DEnVar with the errors of the day and the WRF parameterizations adopted for forecasting. Therefore, the best performance of the WRF model for 24 and 48 h forecast using the initial conditions updated by 3DEnVar occurred due the combination of the analysis updated by 3DEnVar with the errors of the day and the WRF parameterizations adopted for forecasting.

Another interesting fact is that the metrics in Figures 10–12 show that the best performances of the model were proportional to the increase in the length of the forecast (note the BIAS, SR, POD, and FAR best performances in different SMR settings). This finding occurred due to spin-up length (time required for the model to reach its internal equilibrium). Typically, short-term weather forecast models require a 6–12 h spin-up [40].

Nonetheless, none of the forecasts carried out with the analysis of DA systems are evaluated here, and experiments without initial conditions updating indicated the possibility of heavy rain as registered by meteorological stations was only of moderate intensity. One justification is the bad performance of the WRF Cumulus parametrization. In this work, they were chosen based on the [23] work, while another work suggests Kain–Fritsch as the best parametrization for the Brazilian Northeast region [41].

Encouraging results have been obtained in several works over the years by using hybrid assimilation 3DEnVar based on EnSRF and 3DVar. The results presented in these works [16,38] and this study case show that 3DEnVar is an efficient algorithm for improving rainfall forecasts for its study locations. This fact occurs because 3DEnVar updates the analyses with the errors of the day, decreasing the initial condition errors that affect the weather forecast performed by the WRF equations.

4. Conclusions

This work evaluated the 3DVar, the EnSRF, and the 3DEnVar DA impact in the generation of analyses in order to verify their contributions in the heavy rain forecasts in the BNE. We concluded that the inclusion of the errors of the day in the 3DVar (climatological) backgound covariance matrix, i.e, by using the EnSRF and the 3DEnVar, the analysis was improved and it led to a better precipitation forecast.

Throught the RMSE evaluation, we concluded that the WRF model initialized with the initial conditions from 3DEnVar (experiments f24h, f48h, and f72h) for the MCS1 and from EnSRF (24h and f48h experiments) and GEFS (experiment f72h) for the MCS2 (2017) produced the best forecasts. In general, these results shows that the errors of the day considered in the EnSRF and the hybrid ensemble variational background error covariances improved the WRF forecasts.

The contingency table indices also revealed that the WRF model initiated with the 3DEnVar analysis also improved its ability to detect rainfall for different regions in the Maranhão state. However, the heavy rainfall events associated with the MCS over the BNE were underestimated for all evaluated experiments (considering the 24 h accumulated precipitation). The employed cumulus cloud parameterization scheme may have limitations on forecasting heavy rain associated with MCS in the BNE, since all experiments underestimated the heavy precipitation.

The lack of enough conventional temperature, humidity, and pressure data available for being assimilated in the BNE may also have impacted the quality of the model's predictions, despite the best performance of the WRF model initiated with 3DEnVar in SCM1 and with EnSRF in SCM2.

In summary, the results showed that 3DEnVar could improve the WRF 24 h accumulated precipitation forecast, as shown with the MCS1. However, the MCS2 evaluation showed that the WRF model initialized with the EnSRF analysis had better results. Therefore, in order to improve the predictions through the WRF model by considering the 3DEnVar, some solutions are as follows: to create an algorithm that automatically defines the weights assigned to the EnSRF and 3DVar covariance matrix in the GSI hybrid system; an increase in the ensemble size; an increase in model resolution (horizontal and vertical); and an increase in the ensemble state by using some ensemble of model physical parametrizations.

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Abbreviations

The following abbreviations are used in this manuscript:

3DEnVar	3D Ensemble Variational;
3DVar	3D Variational;
BNE	Brazilian Northeast;
CSI	Critical Success Index;
DA	Data Assimilation;
EnSRF	Ensemble Kalman Filter;
FAR	False Alarm;
POD	Probability of Detection;
MCS	Mesoscale Convective System;
RMS	Regional Modeling System;
RMSE	Root Mean Square Error;
SR	Success Rate;
WRF	Weather Research and Forecasting;
GSI	Grid Statistical Interpolation.

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